



# **Quark-Gluon Plasma Physics**

## **9. Quarkonia and Deconfinement**

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# 9.1 Quarkonia

- Quarkonia are heavy quark antiquark bound states, i.e.  $c\bar{c}$  and  $b\bar{b}$
- since masses of charm and beauty quarks are high as compared to QCD scale parameter  $\Lambda_{\text{QCD}} \sim 200 \text{ MeV}$   
non-relativistic Schrödinger equation can be used to find bound states

$$\left(-\frac{\nabla^2}{2(m_Q/2)} + V(r)\right)\Psi(\vec{r}) = E\Psi(\vec{r})$$

with quark-quark potential of the form

$$V(r) = \sigma r - \frac{4}{3} \frac{\alpha_s}{r} + \frac{32\pi\alpha_s}{9} \frac{\vec{s}_1 \cdot \vec{s}_2}{m_Q^2} \delta(\vec{r}) + \dots$$

confinement

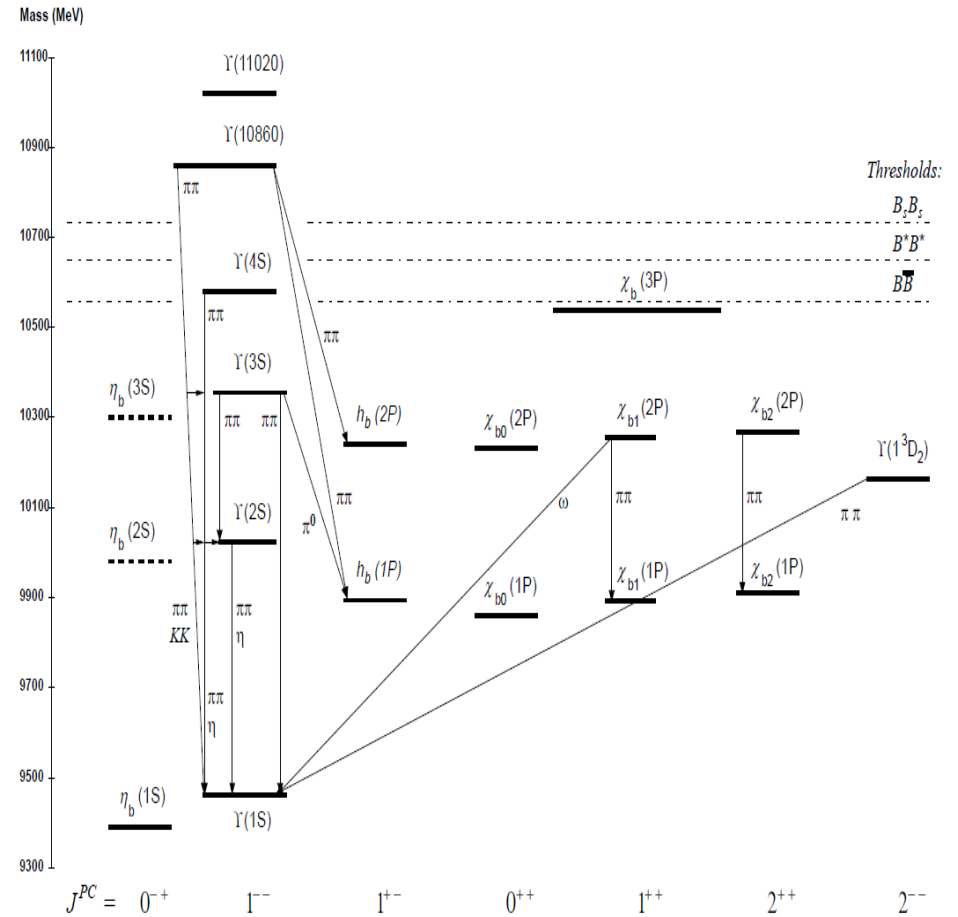
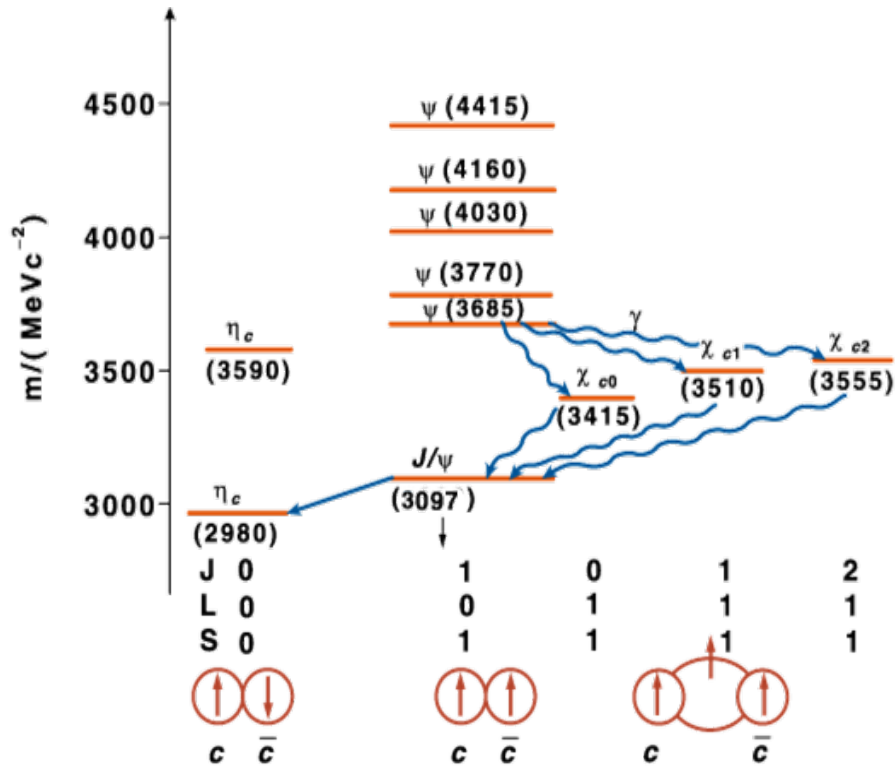
color Coulomb int.

spin-spin int.

tensor, spin-orbit, higher  
order rel. corr.

- with  $\sigma \sim 0.9 \text{ GeV/fm}$ ,  $\alpha_s(m_Q) \sim 0.35$  and  $0.20$  for  $m_c=1.5$  and  $m_b=4.6 \text{ GeV}$   
obtain spectrum of quarkonia

# Charmonium and Bottomonium spectra



color singlet states

## 9.2 Charmonia at finite temperature

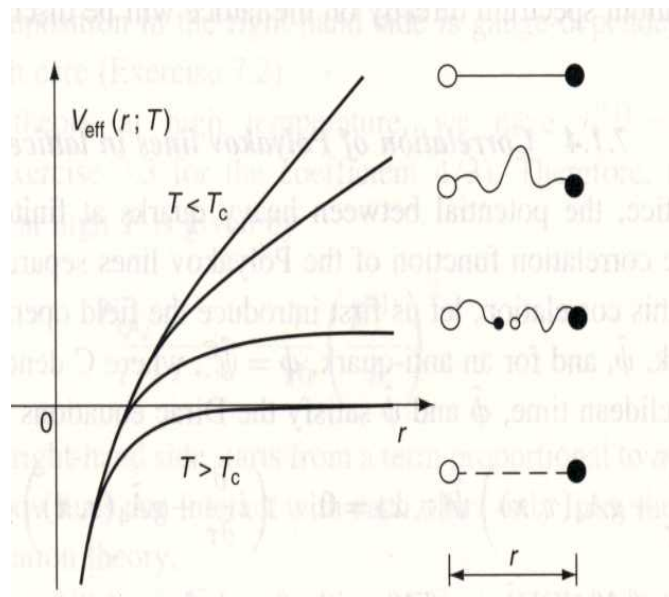
consider  $T \ll m_c$  so QGP of gluons, u,d,s quarks and antiquarks, no thermal heavy quarks

consider  $c\bar{c}$  in thermal environment of gluons and light quarks

$$V(r) \rightarrow V_{eff}(r, T) \quad \text{and} \quad m_Q \rightarrow m_Q(T)$$

in QGP color singlet and color octet  $c\bar{c}$  states can mix by absorption or emission of a soft gluon

→ modification of  $V_{eff}$



- reduced string tension as  $T$  approaches  $T_c$
- string breaking due to thermal  $q\bar{q}$  and gluons leading to  $D$  and  $D\bar{D}$
- for  $T > T_c$  confining part disappears and short range Coulomb part is Debye screened to give Yukawa type potential

$$V_{eff}(r, T) \rightarrow -\frac{4}{3} \frac{\alpha_s}{r} e^{-r/\lambda_D}$$

$$\omega_D = 1/\lambda_D$$

Debye screening mass and length

# Debye screening of quarkonia

unlike Coulomb potential, Yukawa potential does not always have bound states

→ dissociation of quarkonia if  $\omega_D$  sufficiently large at high T

idea: T. Matsui, H. Satz, Phys. Lett. B 178 (1986) 416

compare Bohr radius of charmonia  $r_B$  and Debye screening length  $\lambda_D$

for  $r_B$  smaller than  $\lambda_D$  bound states exist even for  $\sigma=0$   
for  $r_B$  larger than  $\lambda_D$  no bound states

equivalently to QED where  $r_B(\text{hydrogen}) = 1/(m_e\alpha)$  we have:  $r_B = 3/(2m_Q\alpha_s)$   
and the Debye screening mass:

$$\omega_D^2 = \frac{4\pi\hbar c}{3}\alpha_s T^2(N_c + \frac{1}{2}N_f)$$

(see textbooks, e.g. Yagi, Hatsuda, Miake, chapter 4, finite temperature field theory)

bound states then disappear for

$$T \geq 0.15 \times m_Q \sqrt{\alpha_s} \approx 0.16 \text{ GeV for } J/\psi \text{ and } 0.46 \text{ for } \Upsilon$$

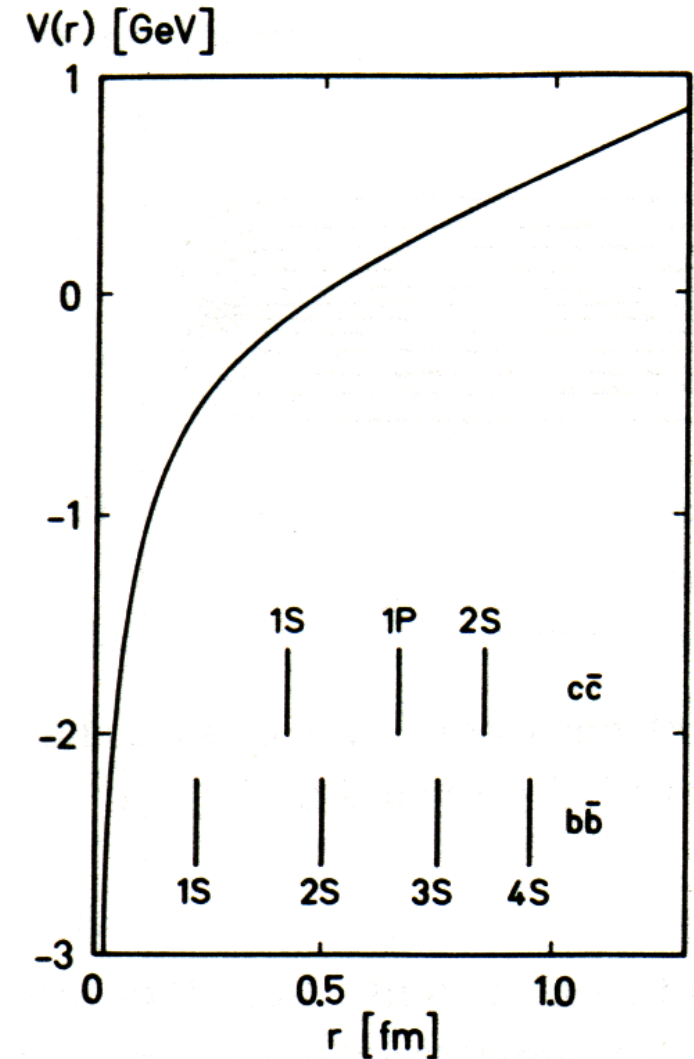
# Different quarkonia melt at different temperatures

using 
$$V(r, T) = \frac{\sigma}{\omega_D(T)} (1 - \exp(-\omega_D(T)r)) - \frac{\alpha}{r} \exp(-\omega_D(T)r)$$

F. Karsch and H. Satz, Z.Physik C51 (1991) 209

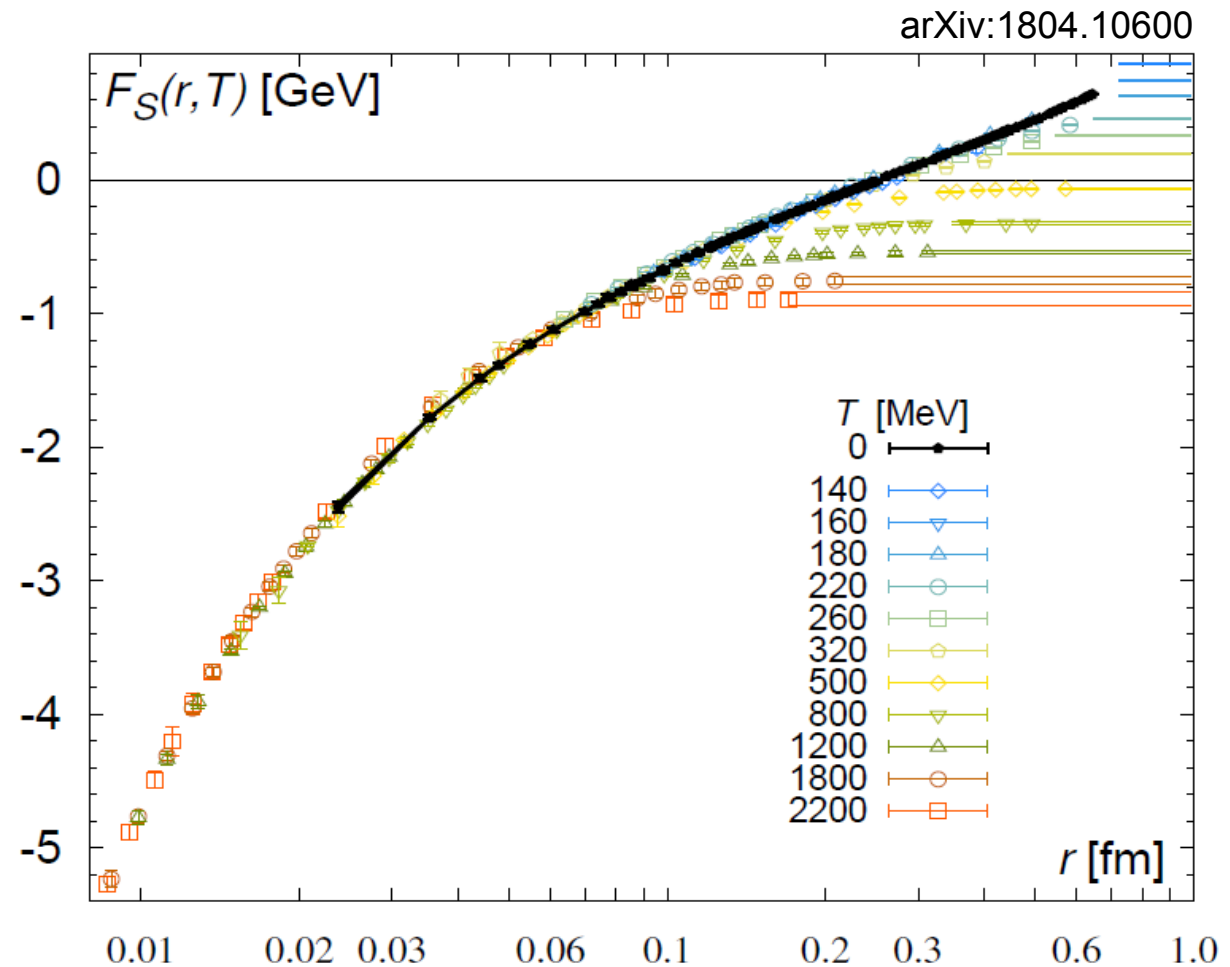
	$J/\psi$	$\psi'$	$\chi_c$	$\Upsilon$	$\Upsilon'$
state	1s	2s	1p	1s	2s
mass(GeV)	3.1	3.7	3.5	9.4	10.0
r (fm)	0.45	0.88	0.70	0.23	0.51
$T_D/T_c$	1.17	1.0	1.0	2.62	1.12
$\epsilon_D$ (GeV/fm <sup>3</sup> )	1.92	1.12	1.12	43.3	1.65

exact values very model dependent, but basic feature:  $J/\psi$ ,  $\psi'$ ,  $\chi_c$ ,  $\Upsilon'$  not bound at or little above  $T_c$ ,  $\Upsilon$  survives longer



# Results on Debye screening from lattice QCD

agree qualitatively, quantitatively after a decade of debate, now some agreement how to extract effective heavy quark potential starting from: color singlet free energy  
general consensus: potential has real and imaginary part



# Hadronization of charm quarks

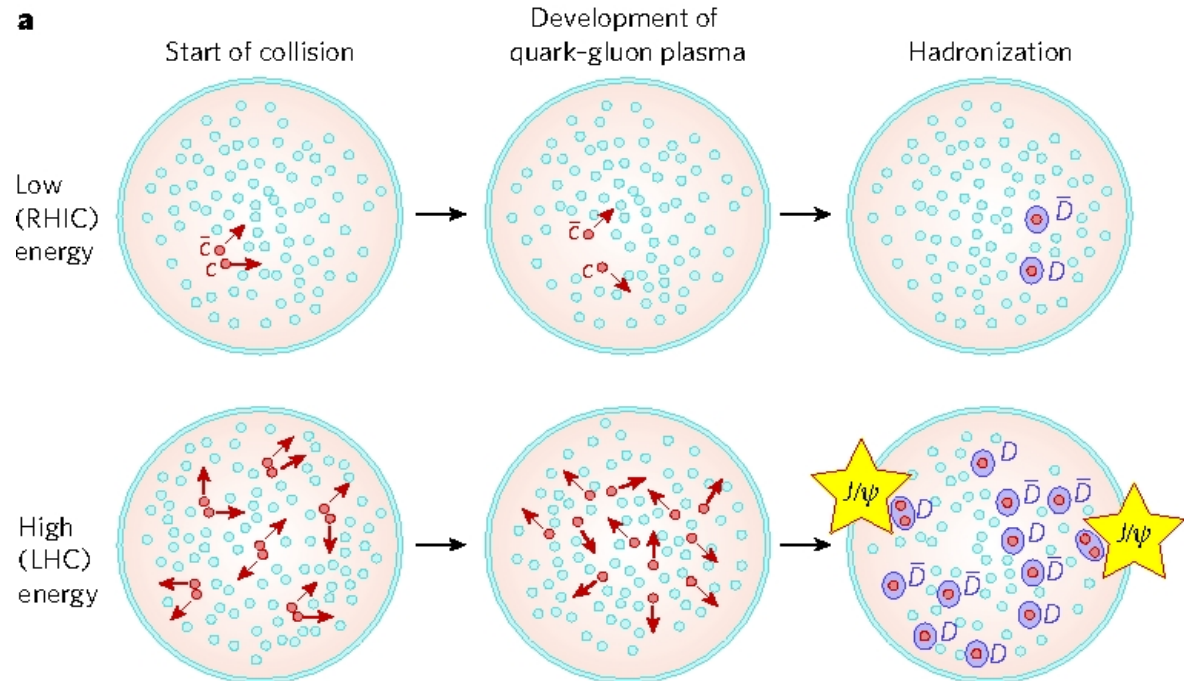
all charm quarks have to appear in charmed hadrons

at hadronization of QGP  $J/\psi$  can form again from deconfined quarks

in particular, if number of  $cc$  pairs is large (colliders) -  $N_{J/\psi} \propto N_{cc}^2$

(P. Braun-Munzinger and J. Stachel, Phys. Lett. B490 (2000) 196)

expect  $J/\psi$  suppression at low  
beam energies (SPS, RHIC)  
and  
 $J/\psi$  enhancement at high  
energies (LHC)






# Extension of statistical model to include charmed hadrons

- assume: all charm quarks are produced in initial hard scattering; number not changed in QGP

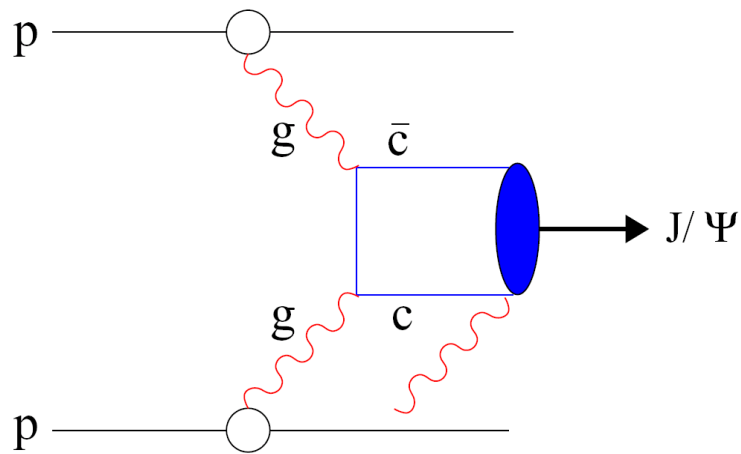
$N_{c\bar{c}}^{direct}$  from data (total charm cross section) or from pQCD

- hadronization at  $T_c$  following grand canonical statistical model used for hadrons with light valence quarks (canonical corr. if needed) technically number of charm quarks fixed by a charm-balance equation containing fugacity  $g_c$

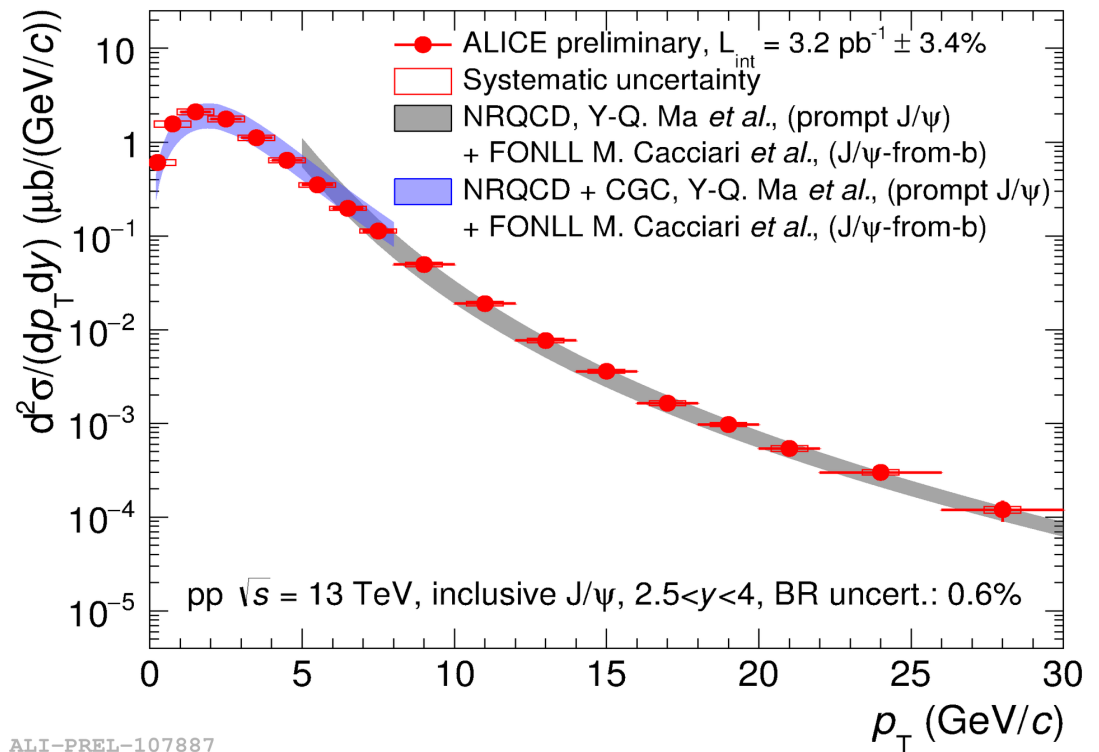
$$N_{c\bar{c}}^{direct} = \frac{1}{2} g_c V \left( \sum_i n_{D_i}^{therm} + n_{\Lambda_i}^{therm} \right) + g_c^2 V \left( \sum_i n_{\psi_i}^{therm} \right) + \dots$$


the only additional free parameter

# 9.3 Production of charmonia in hadronic collisions



- charm and beauty quarks are produced in early hard scattering processes
  - most important Feynman diagram: gluon fusion
  - formation of quarkonia requires transition to a color singlet state
- not pure perturbative QCD anymore, some modelling required  
by now rather successful



ALI-PREL-107887

# Relevant time scales

**formation of  $c\bar{c}$ :** in hard initial scattering on time scale  $1/2m_c$

with  $m_c = 1.3 \text{ GeV} \rightarrow \tau_{c\bar{c}} = 0.08 \text{ fm}/c$

**typical hadron formation time:**  $\tau_{\text{hadron}}$  order 1 fm/c

(Blaizot/Ollitrault 1989 Hufner, Ivanov, Kopeliovich, and Tarasov 2000)

W. Brooks, QM09: description of recent JLAB and HERMES hadron production data in color dipole model  $\rightarrow$  time scale 5 fm/c

**comparable to or longer than QGP formation time:**

$\tau_{\text{QGP}} \cong 1 \text{ fm}/c$  at SPS,  $< 0.5 \text{ fm}/c$  at RHIC,  $\cong 0.1 \text{ fm}/c$  at LHC

at LHC even color octet state not formed before QGP (H.Satz 2006)

$$\tau_8 = 1/\sqrt{2m_c\Lambda_{\text{QCD}}} \approx 0.25 \text{ fm}$$

**collision time:**  $t_{\text{coll}} = 2R/\gamma_{\text{cm}}$  at RHIC 0.1 fm/c, at LHC  $< 5 \cdot 10^{-3} \text{ fm}/c$

# Time scales continued

0.05 fm	0.25 fm
hard	pre-resonance
$\tau_{c\bar{c}} = 1/2m_c$	$\tau_g = 1/\sqrt{2m_c \Lambda_{\text{qcd}}}$

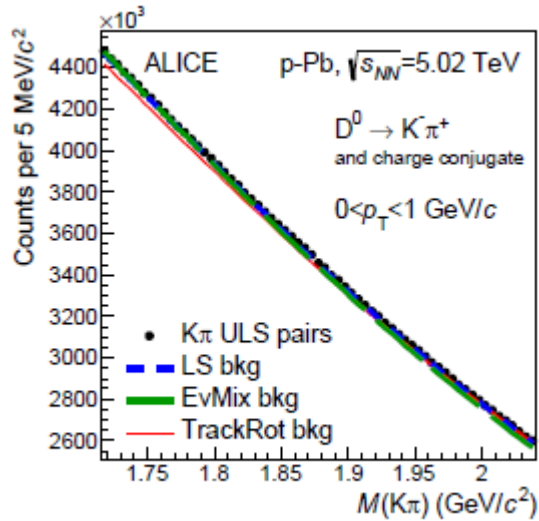
ccbar pairs are formed at collision time scale  $t_{\text{coll}} = \tau_{\text{ccbar}}$

collision time scale comparable to plasma formation time scale and hadron formation time scale at **FAIR** and **SPS**  $t_{\text{coll}} = \tau_{\text{ccbar}} \cong \tau_{\text{QGP}} \cong \tau_{\text{hadron}}$

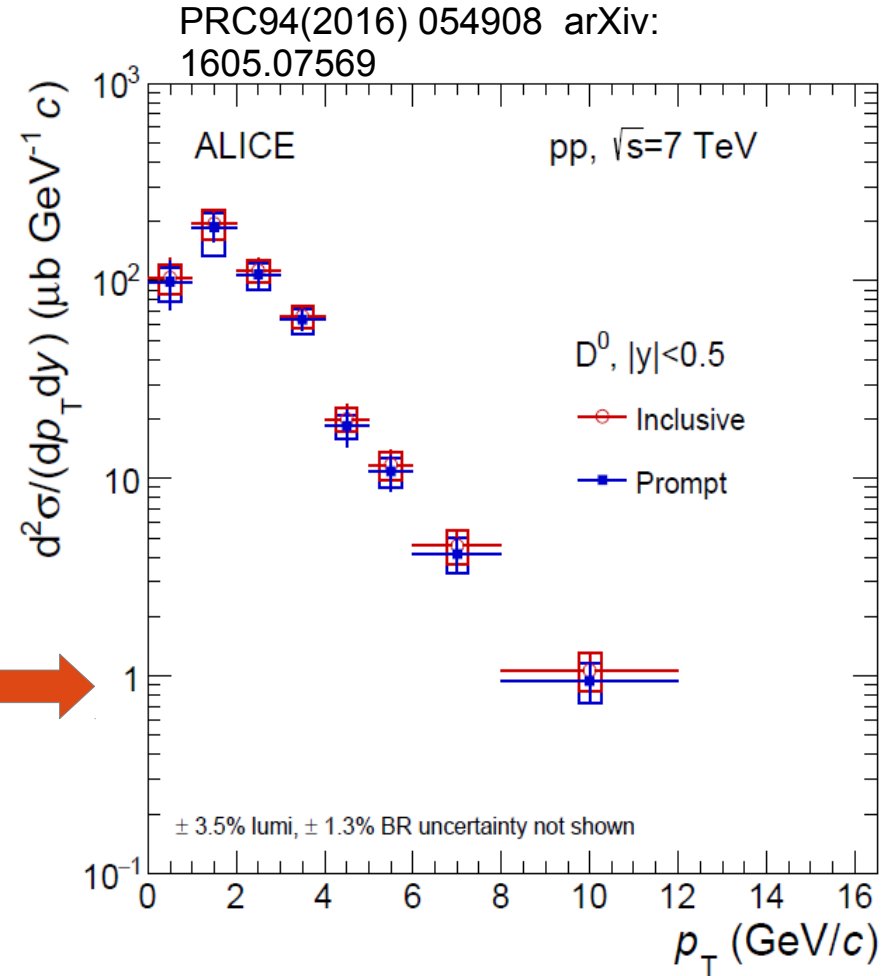
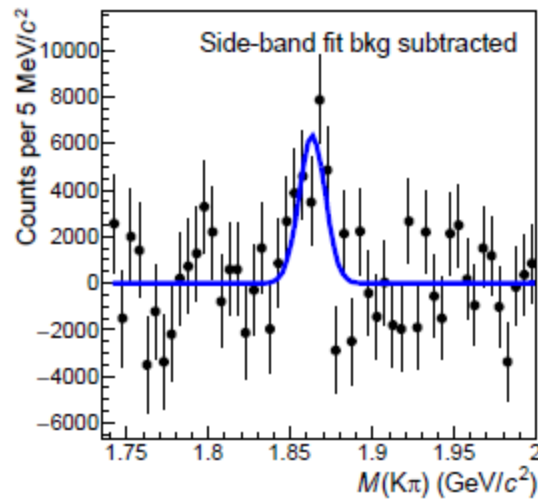
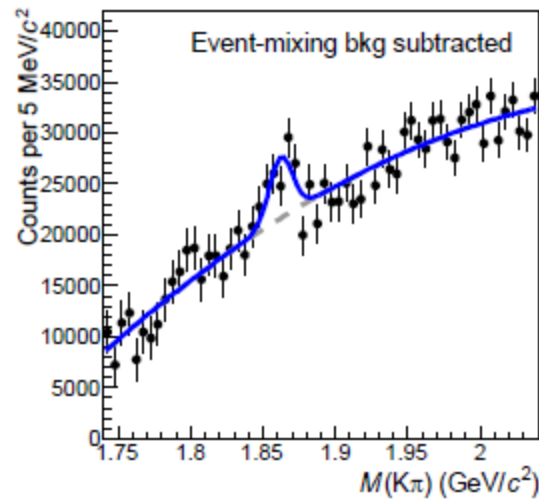
but at **RHIC** and **much more pronounced at LHC** there is the following hierarchy:  $t_{\text{coll}} = \tau_{\text{ccbar}} \ll \tau_{\text{QGP}} \ll \tau_{\text{hadron}}$

expect that cold nuclear matter absorption effects decrease from SPS to RHIC and are totally irrelevant at LHC

# Measurement of total charm production cross section

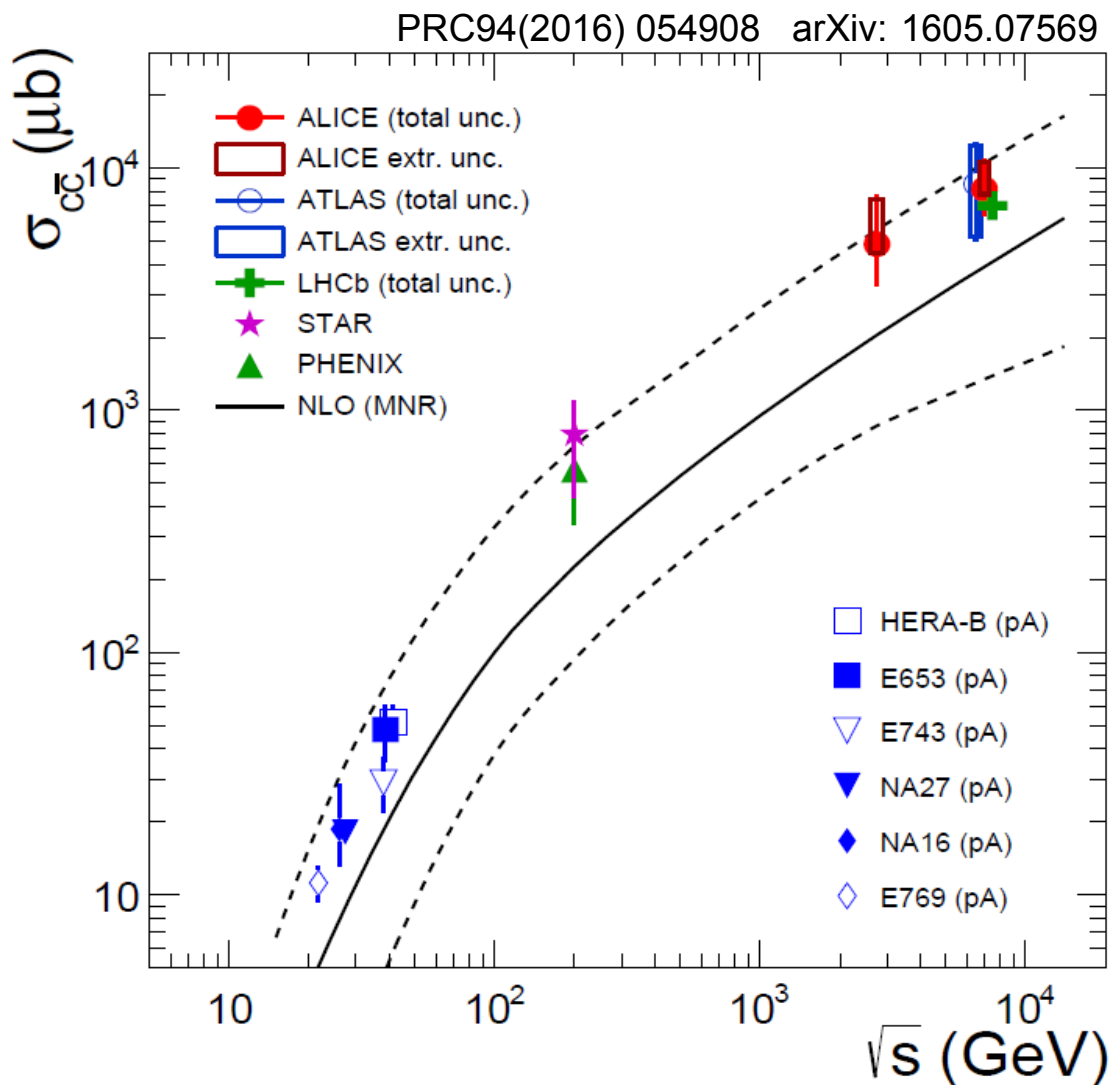


first measurement of cross section down to  $p_T = 0$



very hard struggle to deal with (irreducible) combinatorial background, successful

# the total $c\bar{c}$ cross section in pp at LHC



- good agreement between ALICE, ATLAS and LHCb
- still large syst. error due to extrapolation to low  $p_t$ , need to push measurements in that direction
- data factor  $2 \pm 0.5$  above central value of pQCD but well within uncertainty

## 9.4 Measurement of quarkonia

$$\text{BR}(J/\psi \rightarrow \text{hadrons}) \approx 0.88$$

$$\text{BR}(J/\psi \rightarrow e^+e^-) \approx 0.06$$

$$\text{BR}(J/\psi \rightarrow \mu^+\mu^-) \approx 0.06$$

$$\text{BR}(\psi' \rightarrow \text{hadrons}) \approx 0.98$$

$$\text{of these } \text{BR}(\psi' \rightarrow J/\psi) \approx 0.60$$

$$\text{BR}(\psi' \rightarrow \mu^+\mu^-) \approx 0.008$$

$J/\psi$ ,  $\psi'$  and  $\Upsilon$  via  $e^+e^-$  or  $\mu^+\mu^-$   
 $\chi_c$  very difficult, usually done via

$$\chi_c \rightarrow J/\psi + \gamma$$

of measured  $J/\psi$  typically

$\approx 60\%$  directly produced

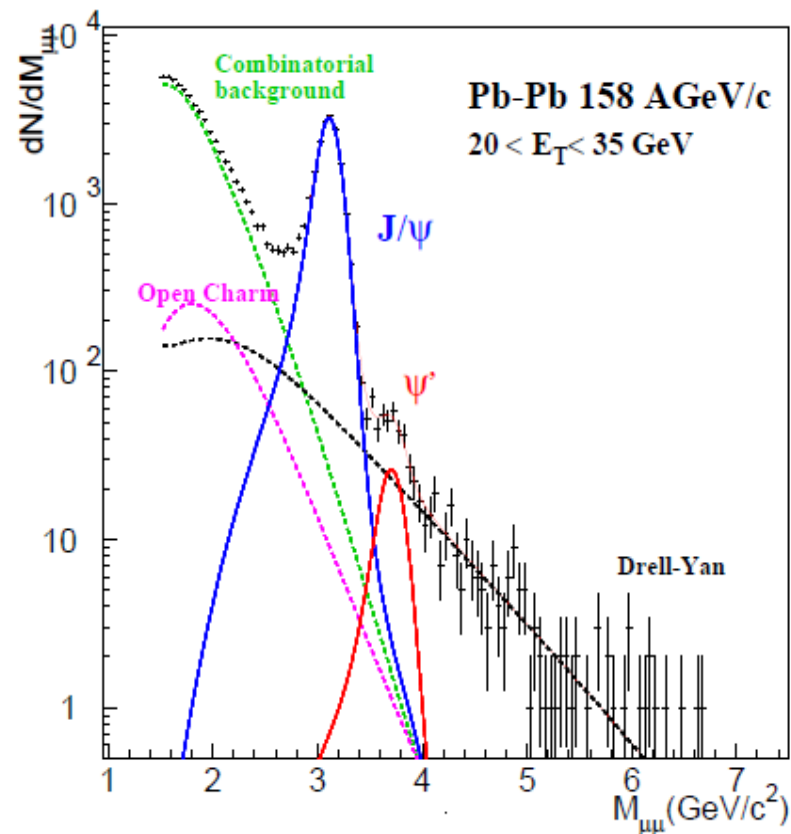
$\approx 10\%$  from  $\psi' \rightarrow J/\psi$

$\approx 30\%$  from  $\chi_c \rightarrow J/\psi$

$$\text{BR}(\Upsilon \rightarrow \text{hadrons}) \approx 0.90$$

$$\text{BR}(\Upsilon \rightarrow e^+e^-) \approx 0.025$$

$$\text{BR}(\Upsilon \rightarrow \mu^+\mu^-) \approx 0.025$$



NA50 at CERN SPS

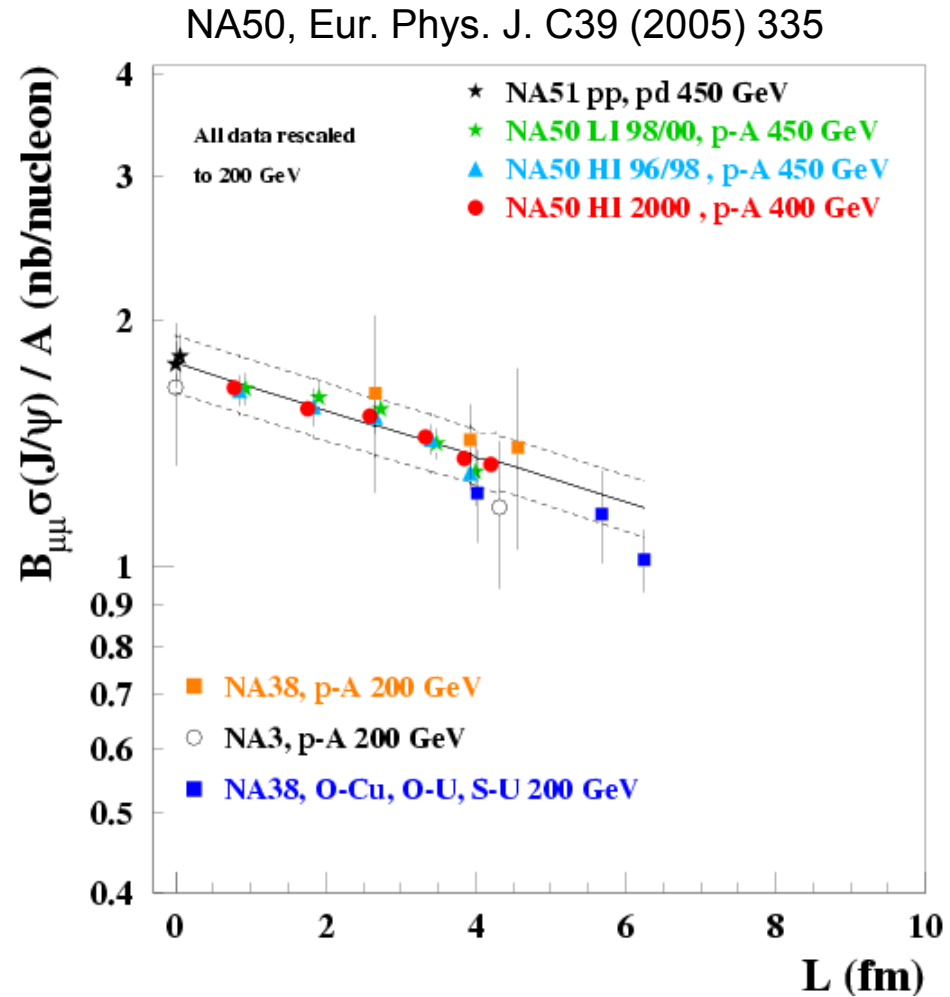
## 9.5 Charmonia in nuclear collisions

in pA collisions at moderate energies (200-450 GeV) universal picture:  
prehadronic state absorbed in nuclear matter

$$\sigma(J/\psi) \propto \exp(-\rho\sigma_{abs}L)$$

with  $\rho = 0.17/\text{fm}^3$   
and  $\sigma_{abs} = 4.1 \pm 0.4\text{mb}$

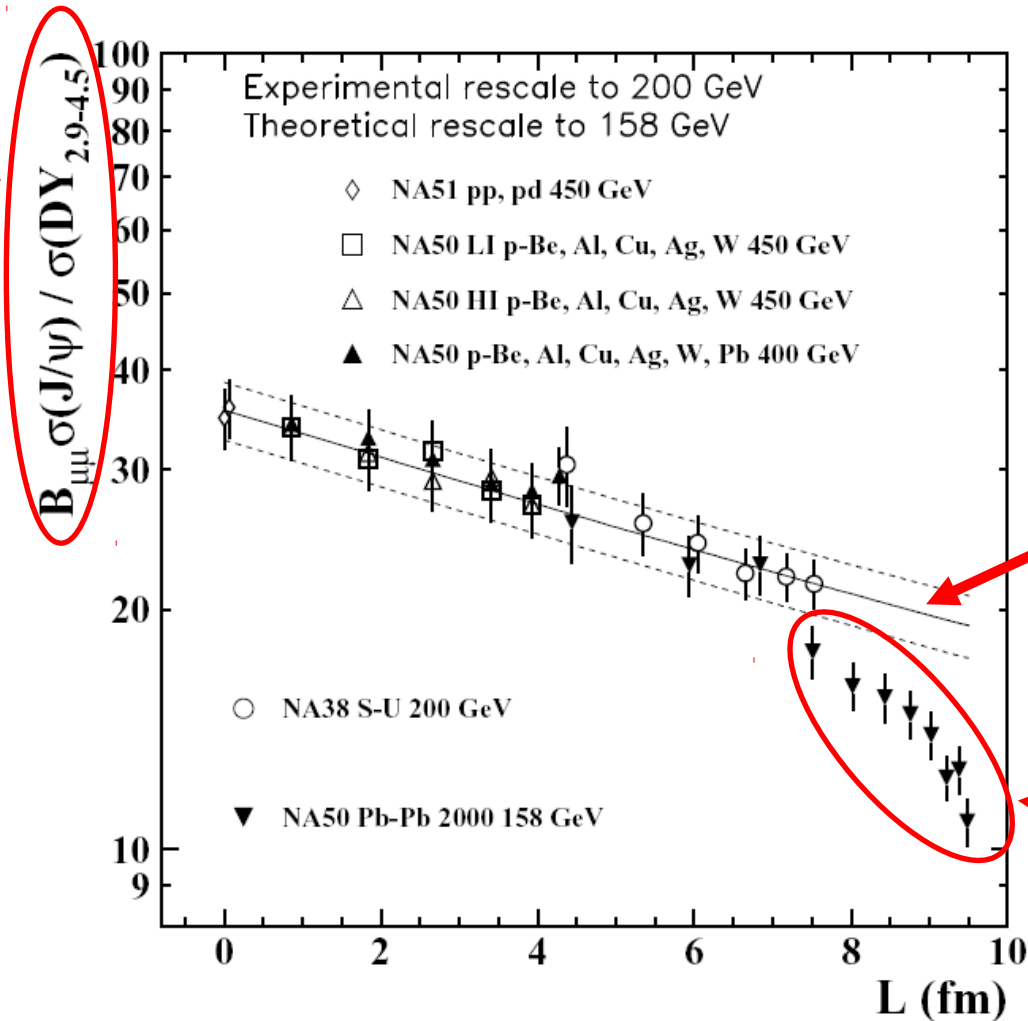
light nuclear collisions follow  
the same picture





# J/psi production in PbPb collisions at SPS energy

normalization  
to Drell-Yan  
process



normal J/psi  
suppression on  
nuclear matter

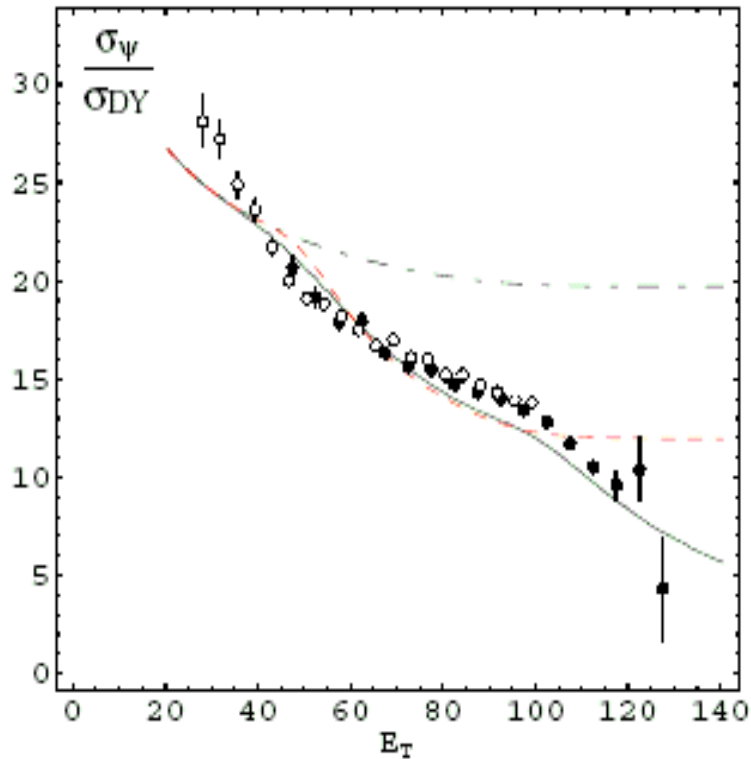
anomalous J/psi  
suppression  
due to QGP?

in central PbPb collisions about 40% less J/psi than expected from pA systematics

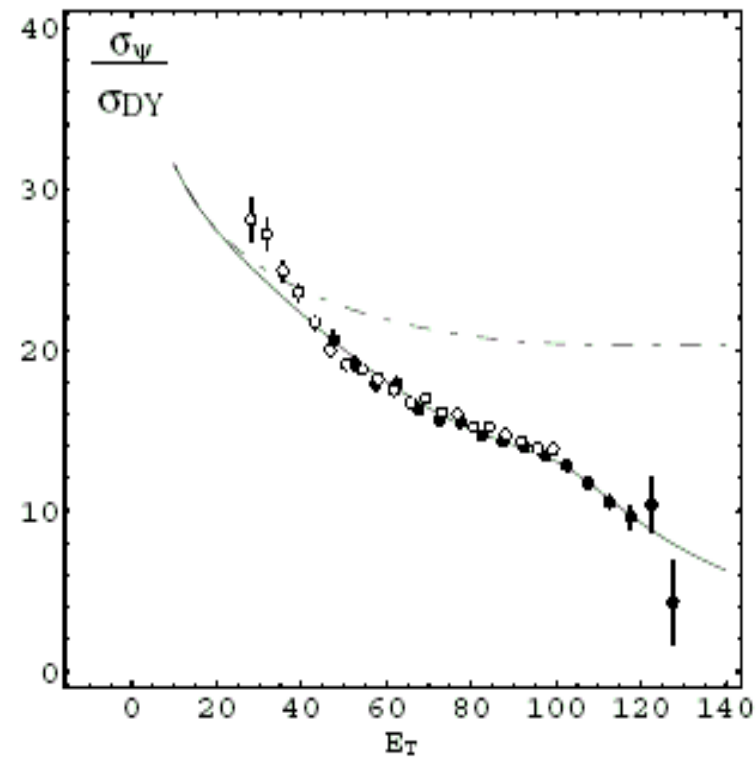
# SPS data consistent with suppression at critical density

dissolution in QGP at critical density  $n_c$  (red dashes) and in addition with energy density fluctuations (solid)

$$n_c = 3.7 / \text{fm}^3$$



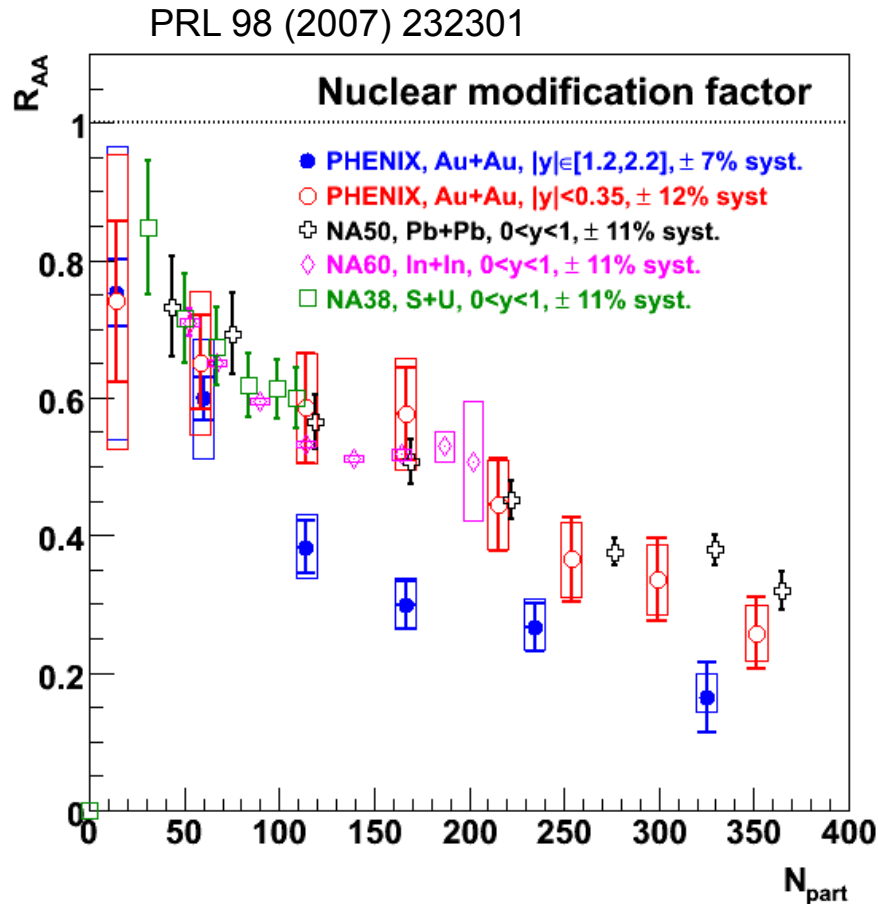
$$n_{c1} = 3.3 \text{ and } n_{c2} = 4.2 / \text{fm}^3$$



→ increasing energy density

J.P. Blaizot, P.M. Dinh, J.Y. Ollitrault, PRL 85 (2000) 4012

# J/psi production in AuAu collisions at RHIC



at mid-rapidity suppression at RHIC very similar to SPS  
 suppression at forward/backward rapidity stronger!

→ but prediction (see above):  
 at hadronization of QGP,  
 J/ψ can form from  
 deconfined quarks, in  
 particular if number of  
 ccbar pairs is large

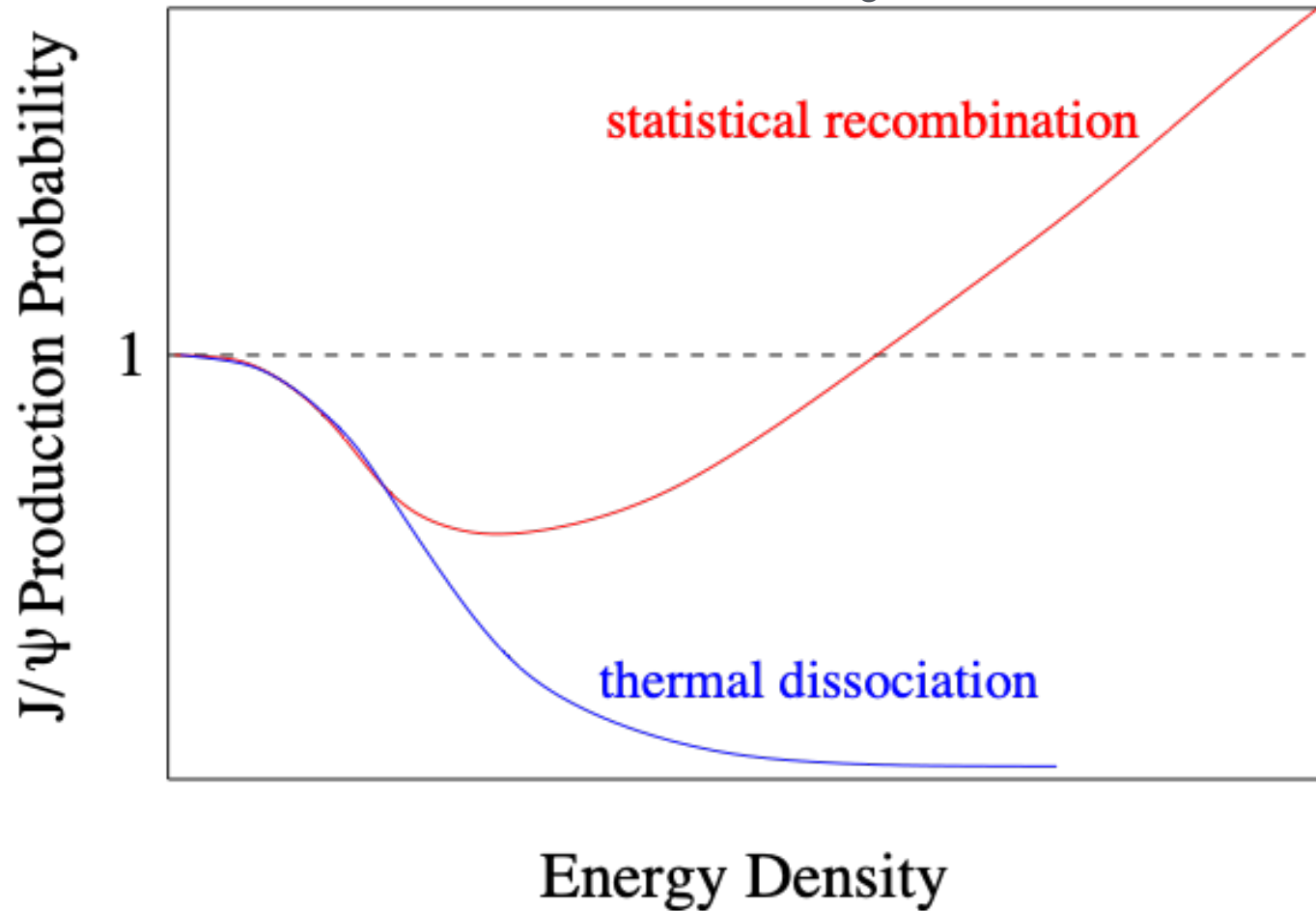
$$N_{J/\psi} \propto N_{cc}^2$$

$$R_{AB} = \frac{dN/dp_T|_{A+B}}{\langle T_{AB} \rangle \times d\sigma_{\text{inv}}/dp_T|_{p+p}},$$

where  $\langle T_{AB} \rangle = \langle N_{\text{coll}} \rangle / \sigma_{\text{inel}}^{\text{NN}}$

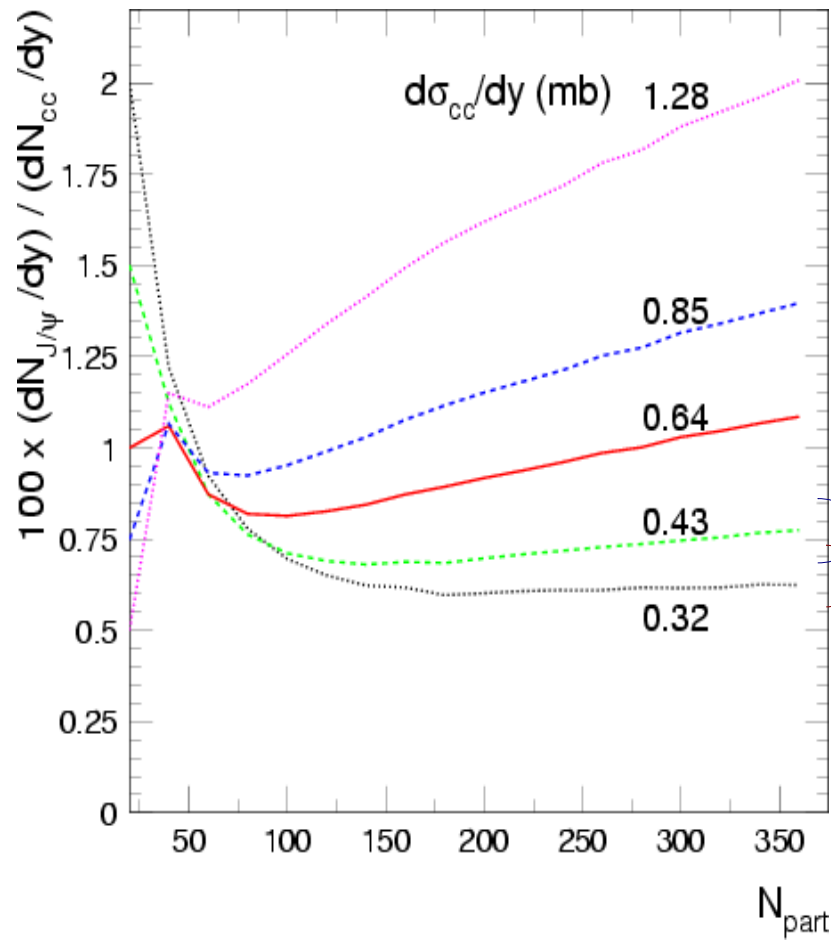
# What to expect for LHC?

Kluberg, Satz, arXiv:0901.3831



# Energy dependence of quarkonium production in statistical hadronization model

A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel Phys. Lett. B652 (2007) 259

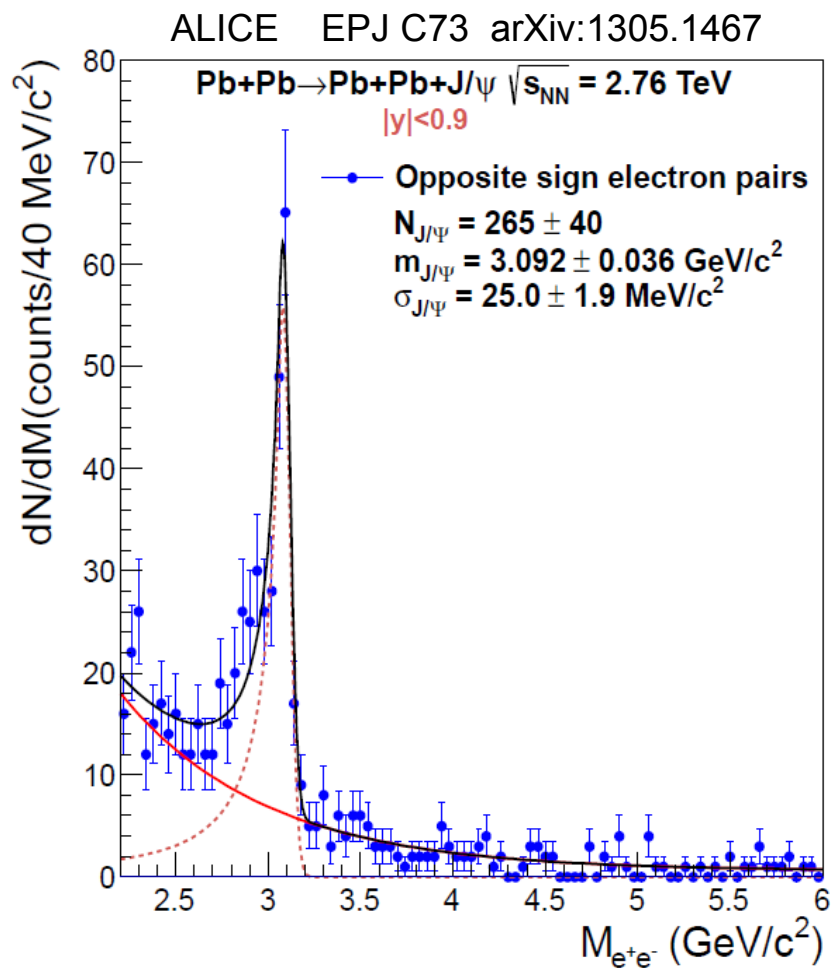


note: stat. model does not make any prediction about **ccbar production cross section**, this is input; depending on ccbar cross section in nuclear collisions at LHC there can be J/psi enhancement

mid-y LHC 2.76 and 5.02 TeV including shadowing

forward-y LHC 2.76 and 5.02 TeV including shadowing

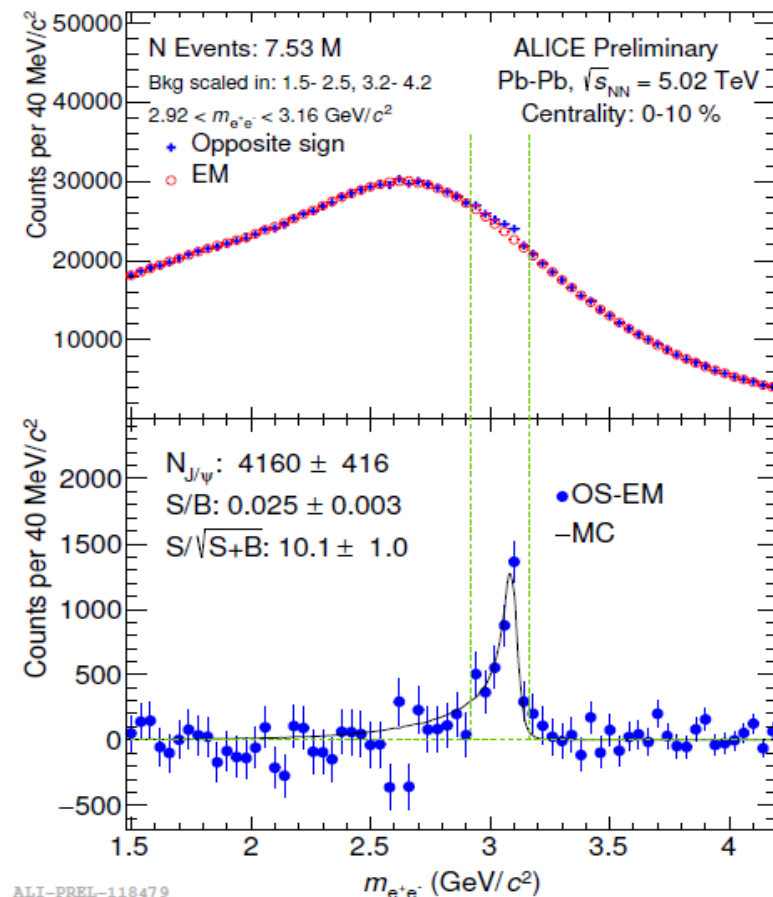
# Reconstruction of J/psi in PbPb collisions at LHC



photoproduction in ultra-peripheral PbPb collisions – excellent signal to background  
 very good understanding of line shape

most challenging: central PbPb collisions in spite of formidable combinatorial background (true electrons, not from J/ψ decay but e.g. D- or B-mesons) resonance well visible

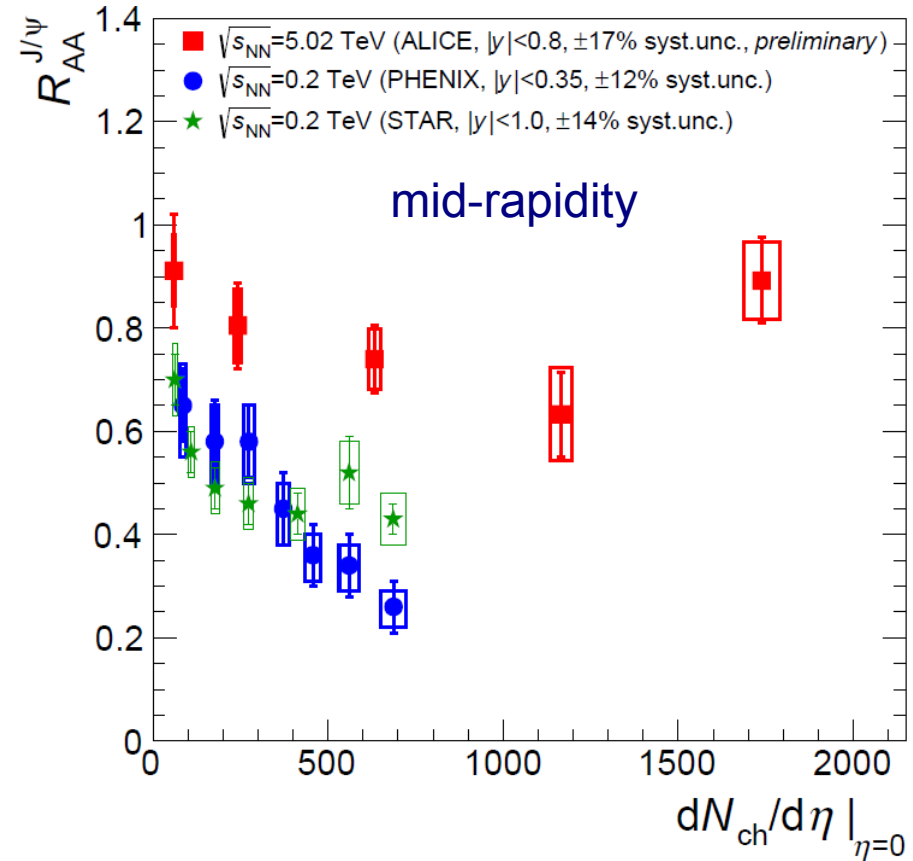
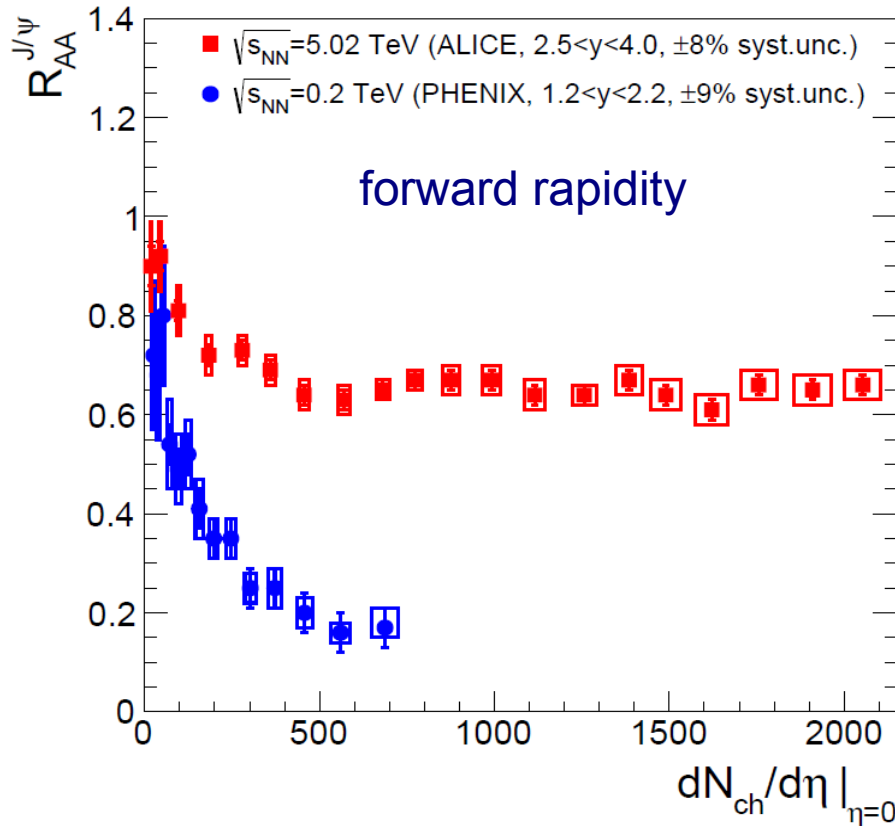
mid  $|y| < 0.8$



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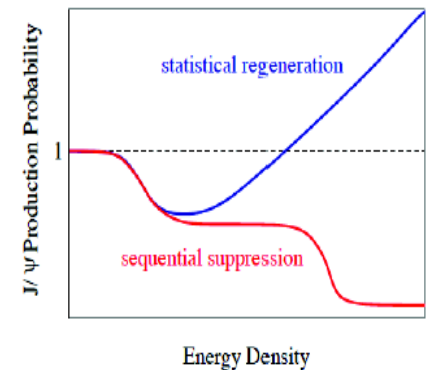
# J/psi production in PbPb collisions: LHC relative to RHIC

$$R_{AA} = \frac{dN^{AA}/dy}{N_{coll} dN^{pp}/dy}$$

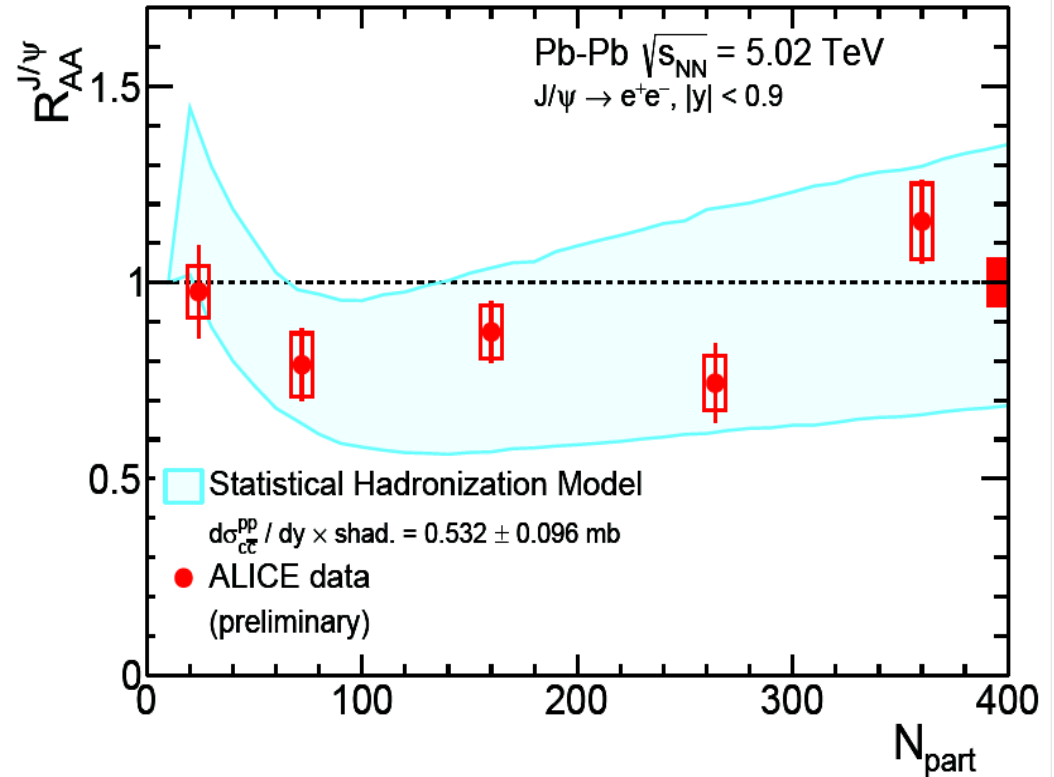
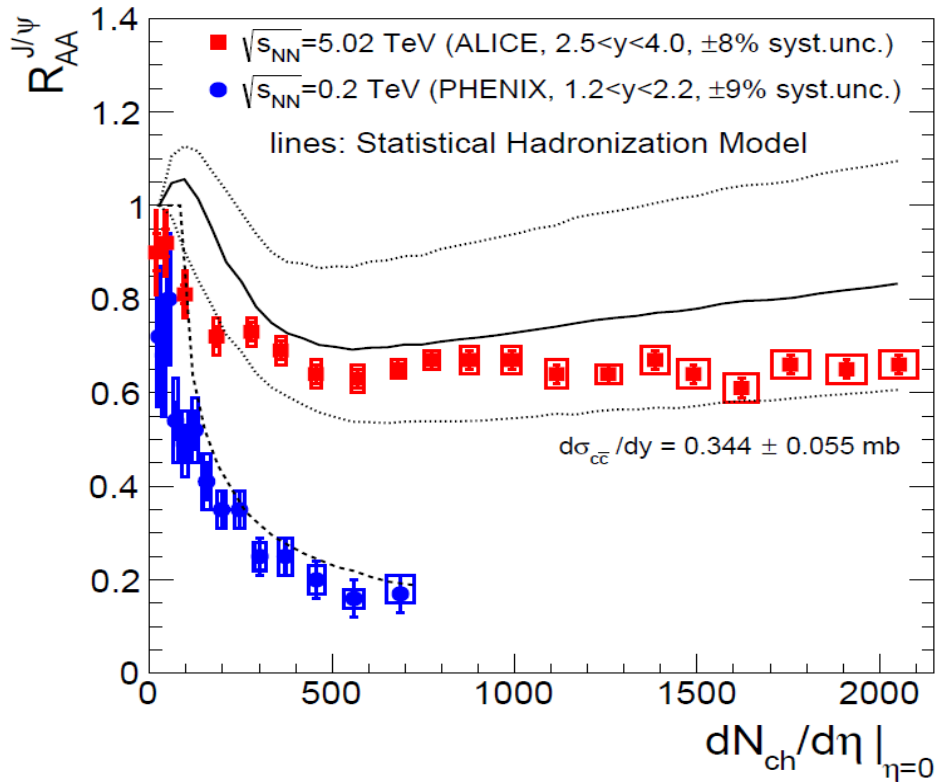


energy density -->

melting scenario not observed  
 rather: **enhancement with increasing energy density!**  
 (from RHIC to LHC and from forward to mid-rapidity)



# J/psi and statistical hadronization

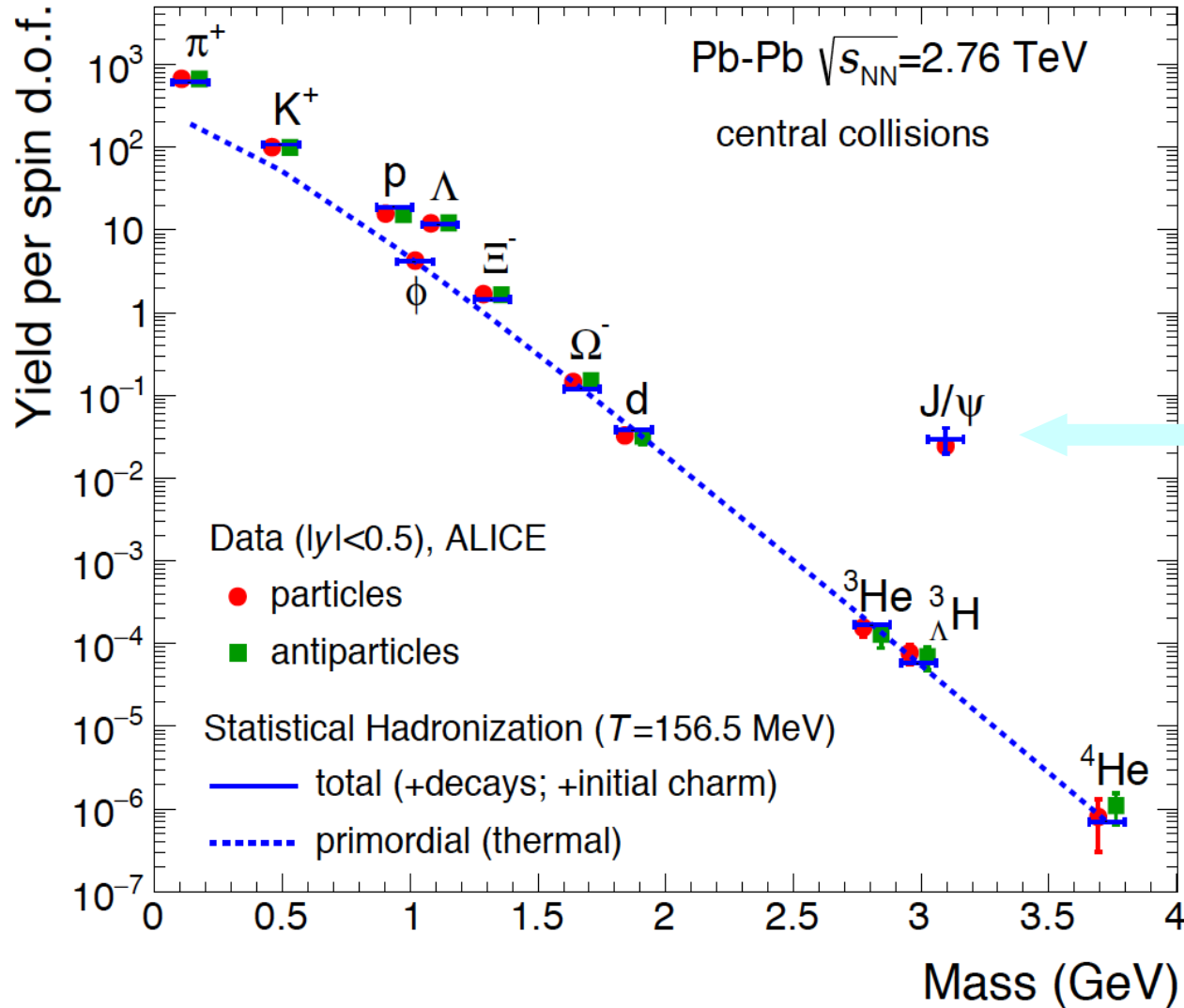


production in PbPb collisions at LHC consistent with deconfinement and subsequent statistical hadronization within present uncertainties

main uncertainties for models: open charm cross section due to shadowing in Pb

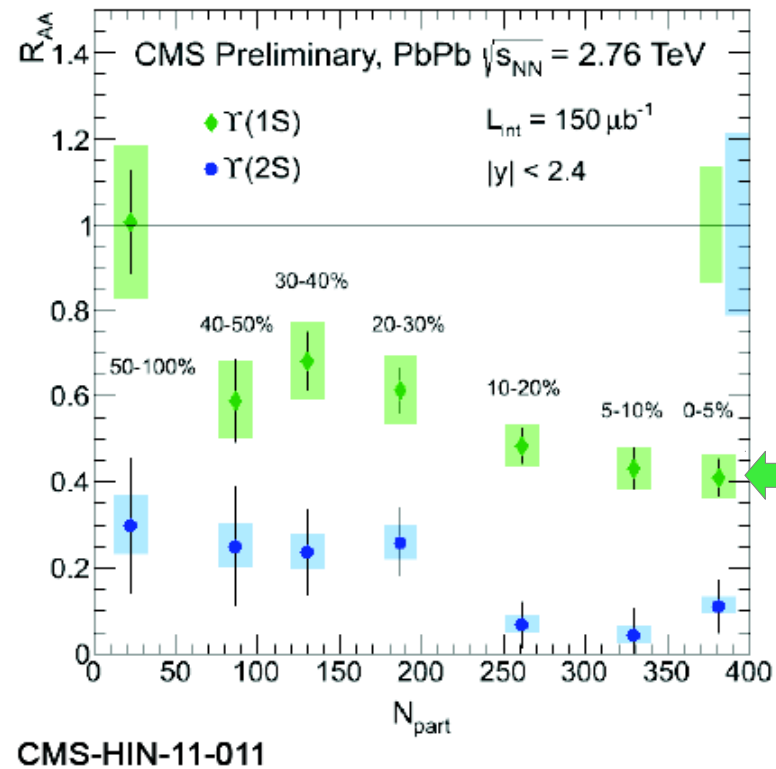
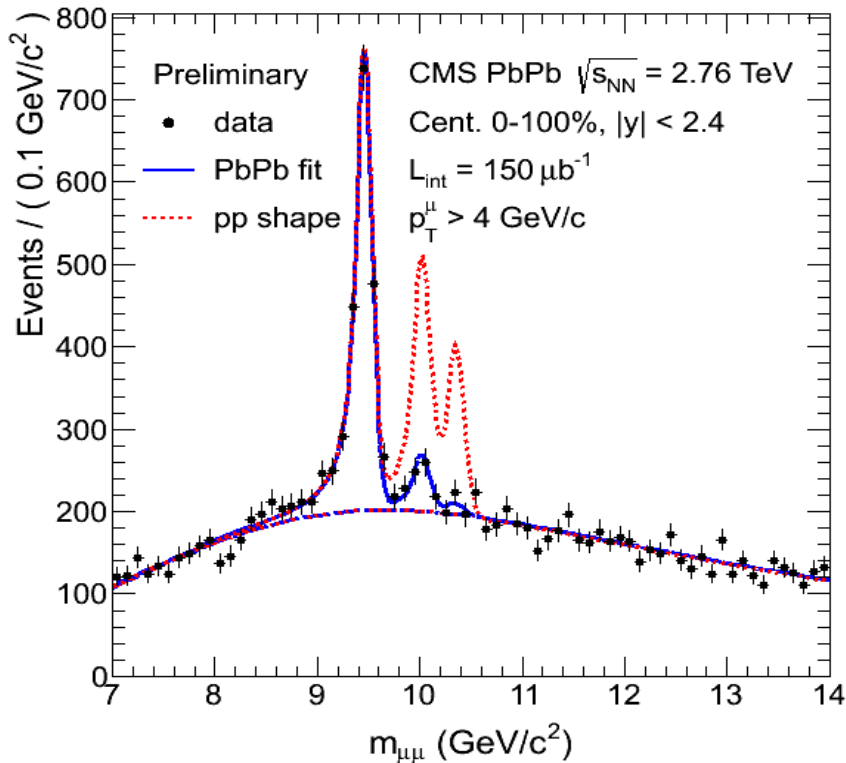


# Systematics of hadron production in SHM



yield exactly reproduced with stat hadr. of deconfined and thermalized c-quarks from initial hard scattering (fugacity)

# First information on Upsilon states for PbPb at LHC



too strong for excited state suppression only (recently established by LHCb)

consistent with expectation that more loosely bound 2S and 3S states are more strongly suppressed

open question today: could also Upsilon form statistically at hadronization? Magnitude of  $R_{AA}$  ok for this