

# High Energy Frontier - Recent Results from the LHC

University of Heidelberg WS 2012/13

## Lecture 3

### **LHC-Searches II**

#### Supersymmetry

# Please Register!

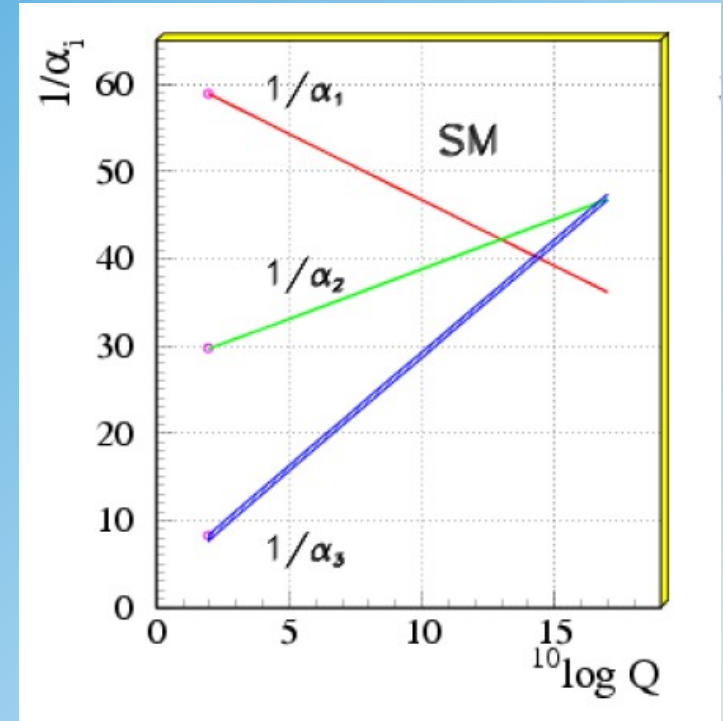
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# Searches for New Symmetries at LHC

- **Fourth generation quarks** (extension of the three generations)
- **Heavy** new vector **bosons** ( $W'$ ,  $Z'$ ) → Left-Right Symmetric Models
- Search for large **extra dimensions** (extension of 3D+1 space-time)
- Search for **supersymmetry**: → fermion-boson symmetry
- and many more models (symmetries) ...
- and many variants ...

# Theory Arguments for New Physics

- (Too) many parameters (25)!
- Why three generations?
- Why so different masses (Yukawa couplings)
- Grand Unification (GUT) → couplings?
- Fine Tuning and Naturalness Problem of the Higgs Mass ( $M_H < M_{\text{planck}}$ )
- Ultraviolet catastrophe at high energies
- Unification with Gravitation?
- Mechanism of CP violation?



	2.4 MeV 2/3 1/3 u up	1.27 GeV 2/3 1/3 c charm	171.2 GeV 2/3 1/3 t top	0 0 1 γ Photon
Quarks	4.8 MeV -1/3 1/3 d down	104 MeV -1/3 1/3 s strange	4.2 GeV -1/3 1/3 b bottom	0 0 1 g Gluon
	<2.2 eV 0 1/2 ν <sub>e</sub> Elektron-Neutrino	<0.17 MeV 0 1/2 ν <sub>μ</sub> Myon-Neutrino	<15.5 MeV 0 1/2 ν <sub>τ</sub> Tau-Neutrino	91.2 GeV 0 1 Z <sup>0</sup> schwache Kraft
Leptonen	0.511 MeV -1 1/2 e Elektron	105.7 MeV -1 1/2 μ Myon	1.777 GeV -1 1/2 τ Tau	80.4 GeV -1 1 W <sup>+</sup> schwache Kraft
				Erdbosonen

electromagnetic ( $\gamma$ )  $\alpha_1 \sim 1/137$   
 weak IA (W, Z)  $\alpha_2 \sim 1/29$   
 strong IA (gluon)  $\alpha_3 \sim 1/10$

# Overview

- Preface
  - Standard Model extensions
  - SU(5)
- Supersymmetry
  - Theory
  - Phenomenology
- Experimental Searches for Supersymmetry

# Beyond the Standard Model

SM Gauge Group (unbroken):

$$SU(3)_{\text{QCD}} \times SU(2)_L \times U(1)_Y$$

Fermions have the following transformation properties:

$$U^a = \begin{pmatrix} u \\ d \end{pmatrix} = (3, 2, 1/6)$$

$$\bar{u} = (\bar{3}, 1, -2/3)$$

$$\bar{d} = (\bar{3}, 1, 1/3)$$

$$L^a = \begin{pmatrix} \nu_e \\ e \end{pmatrix} = (1, 2, -1/2)$$

$$\bar{e} = (\bar{1}, 1, 1)$$

relation to electric charge:  $Q = T_3 + Y$

## Comments:

SM is a real gauge theory (renormalizable)

renormalizability requires:

- same number of quark and lepton families
- conservation of baryon and lepton number

Absence of gauge anomalies requires

- quantized hypercharges (electric charges)

Gauge couplings  $g_1$ ,  $g_2$  and  $g_3$  are different!

# Grand Unification

**Idea: unify couplings**

Complete fermion family fits into a SU(5) group representation

SU(5) with SU(3) x SU(2) embedding of left-handed (chiral) particles

$$\bar{\psi}_i = \begin{pmatrix} d_1^c \\ d_2^c \\ d_3^c \\ e^- \\ \nu \end{pmatrix}, \quad \psi_{ij} = \begin{pmatrix} 0 & u_3^c & -u_2^c & u_1 & d_1 \\ & 0 & u_1^c & u_2 & d_2 \\ & & 0 & u_3 & d_3 \\ & & & 0 & e^+ \\ & & & & 0 \end{pmatrix}.$$

$\{\bar{5}\}$   $\{10\}$

Remark: anti-neutrino can be embedded in SO(10)

# SU(5) Gauge Boson matrix

$$\begin{pmatrix} & & & X_1^{-4/3} & Y_1^{-1/3} \\ \frac{1}{\sqrt{2}} \lambda \cdot \mathbf{V}_{(8)} + \sqrt{\frac{2}{15}} V_{24} & & & X_2^{-4/3} & Y_2^{-1/3} \\ & & & X_1^{-4/3} & Y_3^{-1/3} \\ X_1^{4/3} & X_2^{4/3} & X_3^{4/3} & & \\ Y_1^{1/3} & Y_2^{1/3} & Y_3^{1/3} & \frac{1}{\sqrt{2}} \tau \cdot \mathbf{W} - \sqrt{\frac{3}{10}} V_{24} & \end{pmatrix}$$

$V_8$  corresponds to the gluon fields

$\mathbf{W}$  corresponds to the W field

$V_{24}$  corresponds to the hypercharge field

X, Y correspond to Leptoquarks:  $X, Y \rightarrow l q$  and Diquarks:  $X \rightarrow uu, Y \rightarrow du$



# SU(5) Fermion matrices

New X,Y bosons

$$\lambda_9 = \begin{pmatrix} & 1 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda_{10} = \begin{pmatrix} & -i & 0 \\ 0 & 0 & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\lambda_{11} = \begin{pmatrix} & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}, \quad \lambda_{12} = \begin{pmatrix} & 0 & -i \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix}$$

$$\lambda_{13} = \begin{pmatrix} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda_{14} = \begin{pmatrix} & 0 & 0 \\ 0 & -i & 0 \\ 0 & i & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\lambda_{15} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}, \quad \lambda_{16} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & -i \\ 0 & 0 & 0 \\ 0 & i & 0 \end{pmatrix}$$

$$\lambda_{17} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda_{18} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & i \\ 0 & 0 & 0 \end{pmatrix}$$

$$\lambda_{19} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \lambda_{20} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & i \end{pmatrix}$$

$$\lambda_{20+j} = \begin{pmatrix} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \tau_j \end{pmatrix}, \quad j = 1, 2, 3,$$

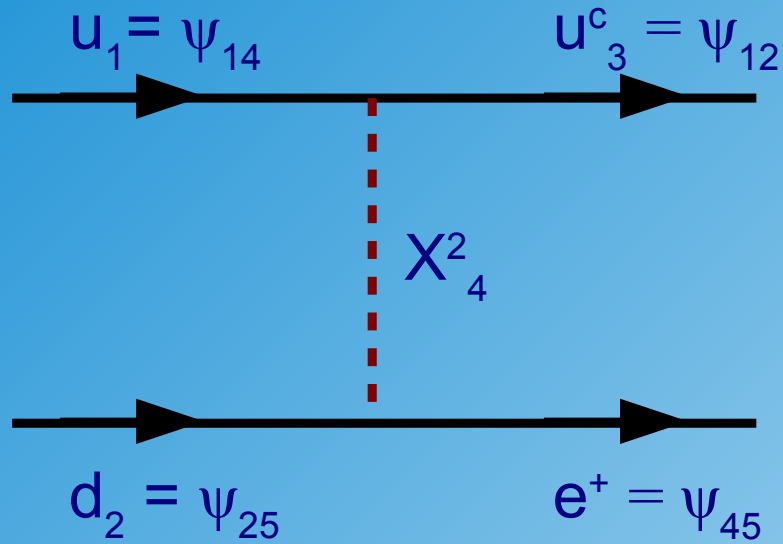
$W^+, W^0, W^-$

$$\lambda_{24} = \frac{2}{\sqrt{15}} \begin{pmatrix} 1 & & & & \\ & 1 & & & \\ & & 1 & & \\ & & & -3/2 & \\ & & & & -3/2 \end{pmatrix}, \quad \text{B-field}$$

gluons

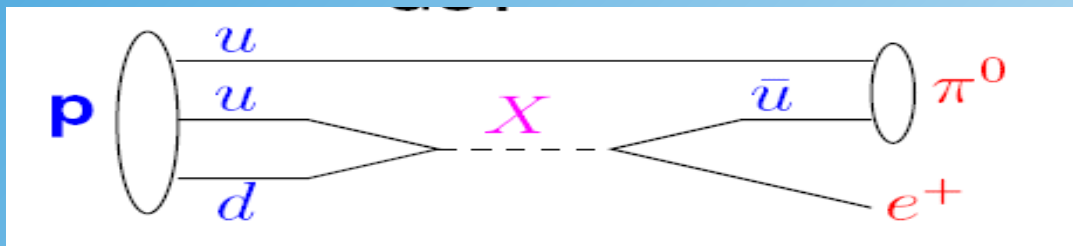
$$\lambda_i = \begin{pmatrix} & 0 & 0 \\ \lambda_i & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad i = 1, \dots, 8,$$

# Baryon/Lepton Number Violation in SU(5)



$$\psi_{ij} = \begin{pmatrix} 0 & u_3^c & -u_2^c & u_1 & d_1 \\ & 0 & u_1^c & u_2 & d_2 \\ & & 0 & u_3 & d_3 \\ & & & 0 & e^+ \\ & & & & 0 \end{pmatrix}$$

## Proton Decay



Lifetime  $\sim 1/M_x^4$

Proton Lifetime  $\gg 10^{30}$  years

$m_x > 10^{15}$  GeV

# Running of Couplings:

Evolve couplings from renormalization group equations:

$$\frac{1}{\alpha_i(\mu)} = \frac{1}{\alpha_i(m)} + \frac{b_i}{2\pi} \log\left(\frac{m}{\mu}\right)$$

with 
$$b_i = -\frac{11}{3}C + \frac{4}{3}N_f l_f + \frac{1}{3}N_s l_s$$

$N_f$  = number of fermions

$N_s$  = number of scalars (Higgs)

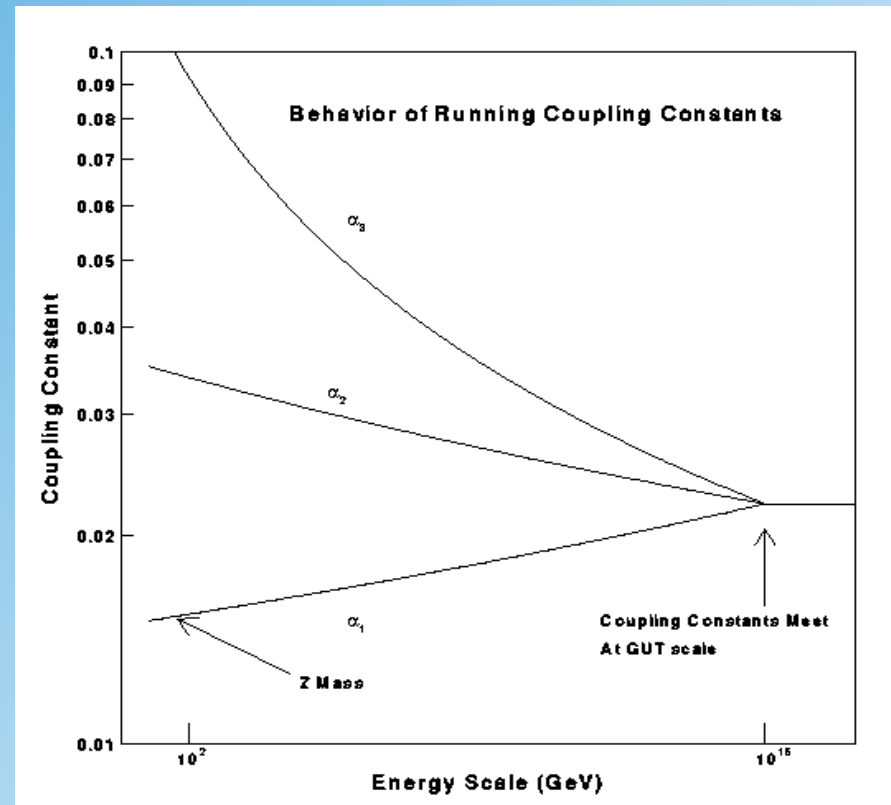
$C$ ,  $l_f$ , and  $l_s$  are quadratic Casimir element of representation

For SU(5) model

$$b_1 = -11 + \frac{4}{3}N_G \quad \leftarrow \text{generations}$$

$$b_2 = -22/3 + \frac{4}{3}N_G + \frac{1}{6}H$$

$$b_3 = \frac{4}{3}N_G + \frac{1}{10}H \quad \leftarrow \text{Higgs doublets}$$



**unification scale below proton lifetime bound !**

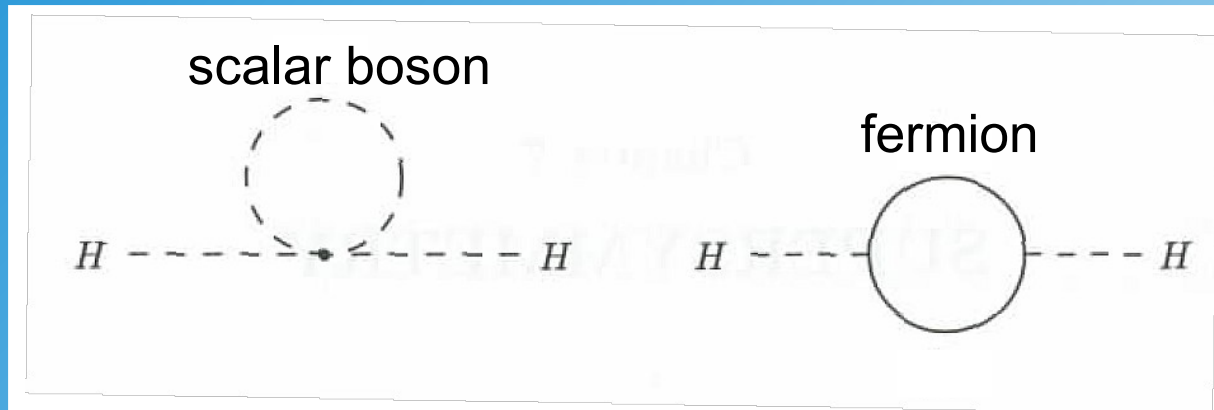
# Lessons from SU(5)

- Unification of coupling possible if right amount of Higgs doublets
- Weinberg angle is more or less correctly predicted  $\sin^2 \theta = 3/8$   
(at unification scale)
- New bosons are predicted with masses  $M_X \sim 10^{15}$  GeV
- Proton is unstable due to new interactions  $X$

# The Hierarchy Problem in the SM

## SM Fine Tuning Problem

The Higgs mass acquires large radiative corrections



$$\delta M_{H_s}^2 = \frac{|\lambda_s|^2}{16\pi^2} \left[ \Lambda^2 + 2m_s^2 \log \Lambda/m_s \right]$$

$$\delta M_{H_f}^2 = \frac{|g_f|^2}{16\pi^2} \left[ -2\Lambda^2 + 6m_f^2 \log \Lambda/m_f \right]$$

note factor 2

In the SM divergences corresponding to physical objects are renormalized. However, the ratio of bare Higgs mass to the observed Higgs mass of

$$M_{\text{Higgs}} / M_{\text{Planck}} = 10^{-17}$$

$$\delta M_H^2 = M_{H, \text{bare}}^2 + \delta M_H^2$$

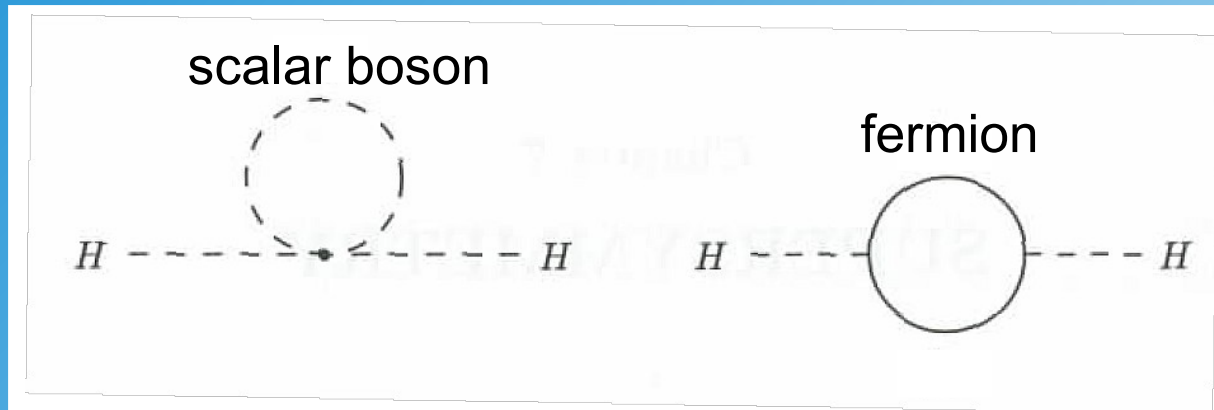
is considered to be unnatural → fine tuning problem

In SUSY the quadratic divergences from fermion loops are compensated by scalars. Only “usual” logarithmic divergences remain.

# The Hierarchy Problem in the SM

## SM Fine Tuning Problem

The Higgs mass acquires large radiative corrections



$$\delta M_{Hs}^2 = \frac{|\lambda_s|^2}{16\pi^2} \left[ \Lambda^2 + 2m_s^2 \log \Lambda/m_s \right]$$

$$\delta M_{Hf}^2 = \frac{|g_f|^2}{16\pi^2} \left[ -2\Lambda^2 + 6m_f^2 \log \Lambda/m_f \right]$$

note factor 2

**An exact cancellation happens if the number of scalars is twice the number of fermions**

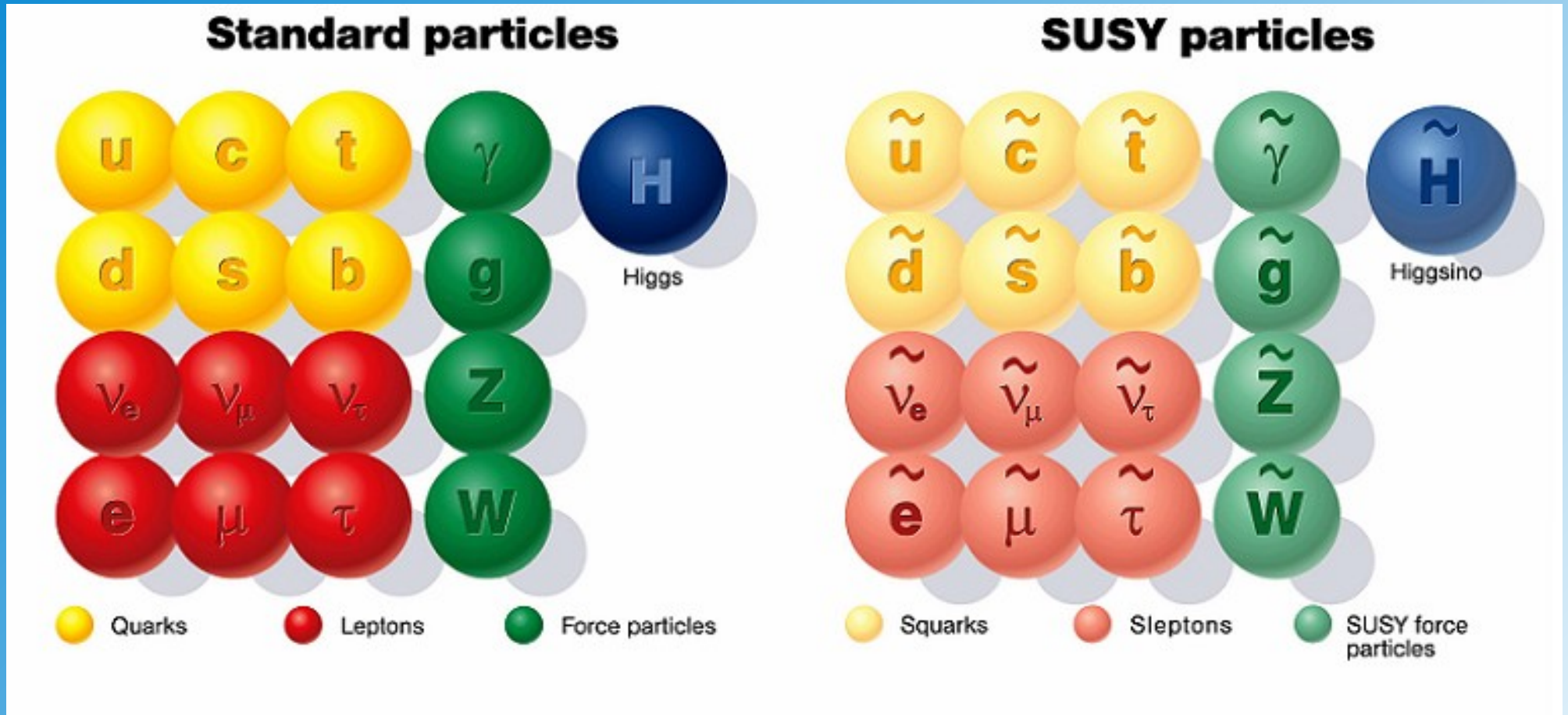
invent symmetry:

**2 x # scalars ↔ # fermions**

# Superpartners

- Supersymmetry (SUSY) connects SM particles with SUSY partners
- SUSY partners are different from SM particles only in spin by  $-1/2$ . All other quantum numbers are identical
- SUSY is broken because we haven't seen SUSY particles yet (different mass of SM and SUSY particles)
- SUSY particles are SM partners with respect to the SM chiral particles and denoted in the following way:  
$$e_L \rightarrow \tilde{e}_L$$
$$e_R \rightarrow \tilde{e}_R$$
- To each SM fermion correspond two SUSY particles!

# Superpartners



actually, there are two Higgs doublets  $\rightarrow$  4 Higgs states!

- SUSY partners not seen (heavy)  $\rightarrow$  SUSY is broken
- SUSY Breaking Scale should be  $\sim 1$  TeV otherwise hierarchy problem reappears



# Superpartners

Table 8.1 *Chiral supermultiplet fields in the MSSM.*

Names		spin 0	spin 1/2	SU(3) <sub>c</sub> , SU(2) <sub>L</sub> , U(1) <sub>y</sub>
squarks, quarks (× 3 families)	$Q$	$(\tilde{u}_L, \tilde{d}_L)$	$(u_L, d_L)$ or $(\chi_u, \chi_d)$	<b>3, 2, 1/3</b>
	$\tilde{u}$	$\tilde{u}_L = \tilde{u}_R^\dagger$	$\tilde{u}_L = (u_R)^c$ or $\chi_{\tilde{u}} = \psi_u^c$	$\bar{\mathbf{3}}, \mathbf{1}, -4/3$
	$\tilde{d}$	$\tilde{d}_L = \tilde{d}_R^\dagger$	$\tilde{d}_L = (d_R)^c$ or $\chi_{\tilde{d}} = \psi_d^c$	$\bar{\mathbf{3}}, \mathbf{1}, 2/3$
sleptons, leptons (× 3 families)	$L$	$(\tilde{\nu}_{eL}, \tilde{e}_L)$	$(\nu_{eL}, e_L)$ or $(\chi_{\nu_e}, \chi_e)$	<b>1, 2, -1</b>
	$\tilde{e}$	$\tilde{e}_L = \tilde{e}_R^\dagger$	$\tilde{e}_L = (e_R)^c$ or $\chi_{\tilde{e}} = \psi_e^c$	<b>1, 1, 2</b>
Higgs, Higgsinos	$H_u$	$(H_u^+, H_u^0)$	$(\tilde{H}_u^+, \tilde{H}_u^0)$	<b>1, 2, 1</b>
	$H_d$	$(H_d^0, H_d^-)$	$(\tilde{H}_d^0, \tilde{H}_d^-)$	<b>1, 2, -1</b>

Table 8.2 *Gauge supermultiplet fields in the MSSM.*

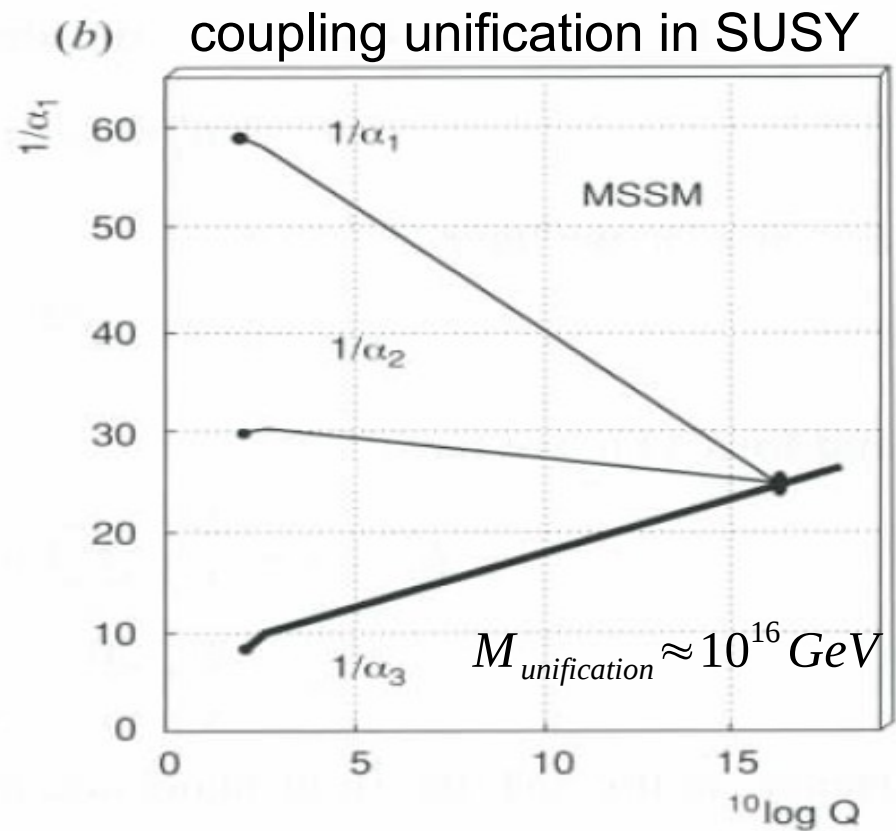
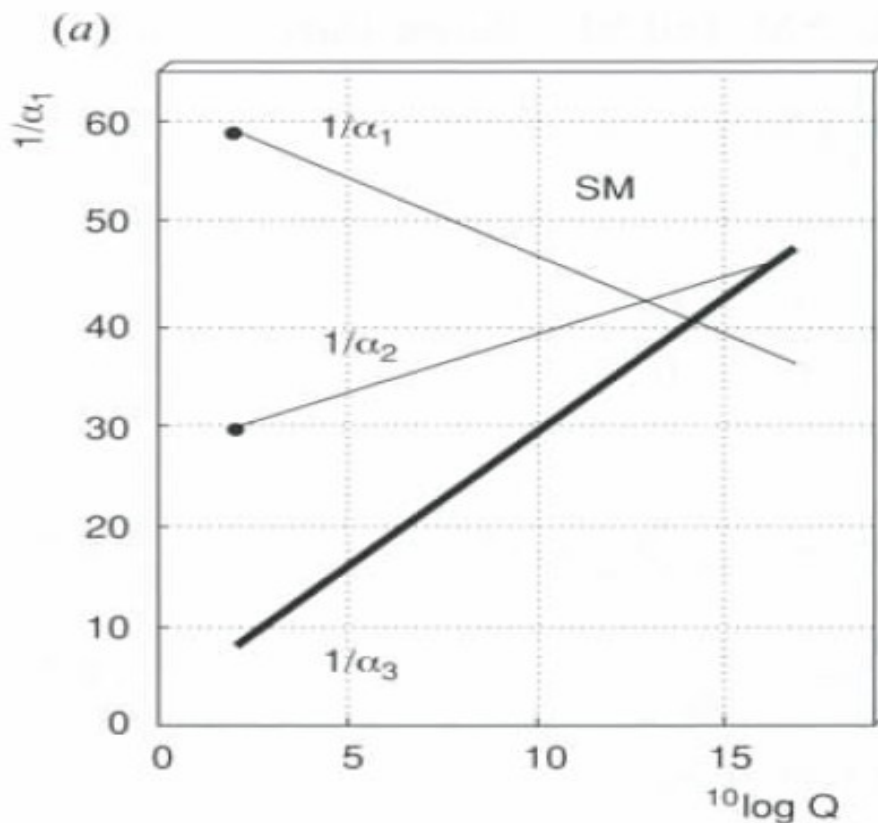
Names	spin 1/2	spin 1	SU(3) <sub>c</sub> , SU(2) <sub>L</sub> , U(1) <sub>y</sub>
gluinos, gluons	$\tilde{g}$	$g$	<b>8, 1, 0</b>
winos, W bosons	$\tilde{W}^\pm, \tilde{W}^0$	$W^\pm, W^0$	<b>1, 3, 0</b>
bino, B boson	$\tilde{B}$	$B$	<b>1, 1, 0</b>

# SUSY Gauge Coupling Unification

logarithmic slopes:

$$\text{SM: } \vec{b}^{SM} = (41/10, -19/6, -7)$$

$$\text{SUSY: } \vec{b}^{SM} = (33/5, 1, -3)$$



# Problems solved by SUSY?

- **(Too) many parameters (25)!**
- **Why three generations?**
- **Why so different masses (Yukawa couplings)**
- **Grand Unification (GUT) → couplings?**
- **Fine Tuning and Naturalness Problem of the Higgs Mass**  
( $M_H < M_{\text{planck}}$ )
- **Ultraviolet catastrophe at high energies**
- **Unification with Gravitation?**
- **Mechanism of CP violation?**

# What breaks SUSY?

Different models developed:

- SuperGravity SUSY-Breaking (SUGRA)
- Gauge Mediated SUSY-Breaking (GMSB)
- Anamolous Mediated Gravity SUSY-Breaking (AMSB)
- ....

# How many Parameters in SUSY?

**too many!**

- 124 parameters in Minimal SUSY Model (MSSM)

Simplified models often used:

- constrained MSSM
- Supergravity models (mSUGRA)
- ...

SUSY breaking and the large number of parameters are concerns!

# MSSM Parameters

- Couplings:  $g_s, g, g'$  corresponding to the  $SU(3) \times SU(2) \times U(1)$  gauge groups
- Higgsino mass parameter  $\mu$
- Higgs-Fermion Yukawa coupling  $y_u, y_d, y_e$  (fermion-Higgs, sfermion-Higgsino)

## SUSY breaking parameters:

### Masses:

- gaugino masses  $M_3, M_2, M_1$  associated to  $SU(3) \times SU(2) \times U(1)$
- scalar squared mass parameters

$$M_{\tilde{Q}}^2, M_{\tilde{U}}^2, M_{\tilde{D}}^2, M_{\tilde{L}}^2, M_{\tilde{E}}^2 \quad \text{corresponding to} \quad (u, d)_L, u_L^c, d_L^c, (\nu, e^-)_L, e_L^c$$

- trilinear Higgs-sfermion-sfermion couplings:  $A_u, A_d, A_e$
- scalar Higgs mass parameters:  $m_1^2 + \mu^2, m_2^2 + \mu^2, m_{12}^2 = B\mu$

$$\text{can also be re-expressed by:} \quad \tan \beta = v_u / v_d \quad v_u^2 + v_d^2 = (246 \text{ GeV})^2$$

**In total 124 parameters in MSSM**

# SUSY Phenomenology

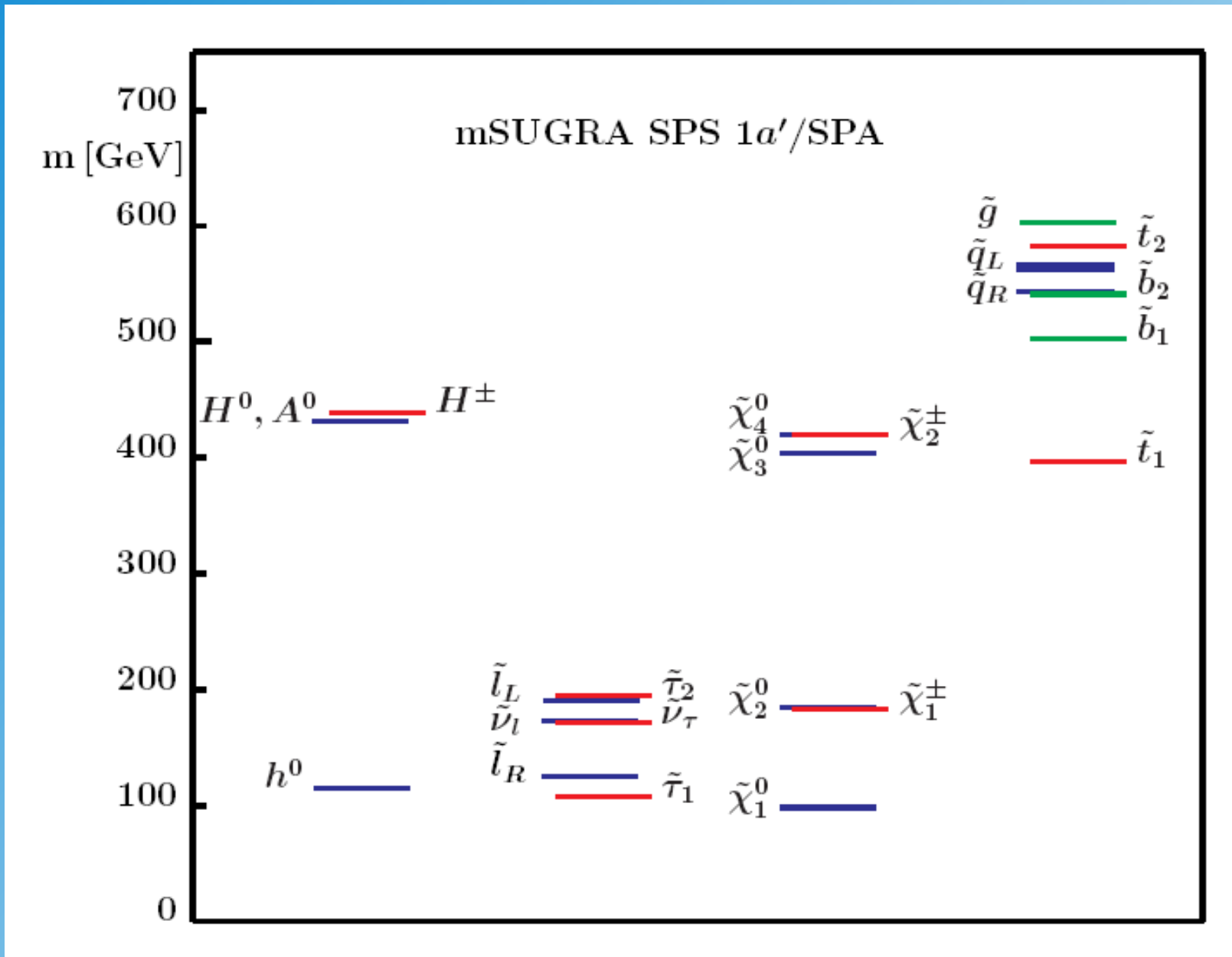
- particle spectrum is rich and complicated
- several particles can mix!

$$\tilde{B}, \tilde{W}^0, \tilde{H}, \tilde{h} \rightarrow \chi_1^0, \chi_2^0, \chi_3^0, \chi_4^0 \quad \text{neutralinos}$$

$$W^\pm, H^\pm \rightarrow \chi_1^\pm, \chi_2^\pm \quad \text{charginos}$$

Masses of states depend on SUSY-breaking scheme and parameters

# SUSY Mass Phenomenology





# SUSY Mass Phenomenology

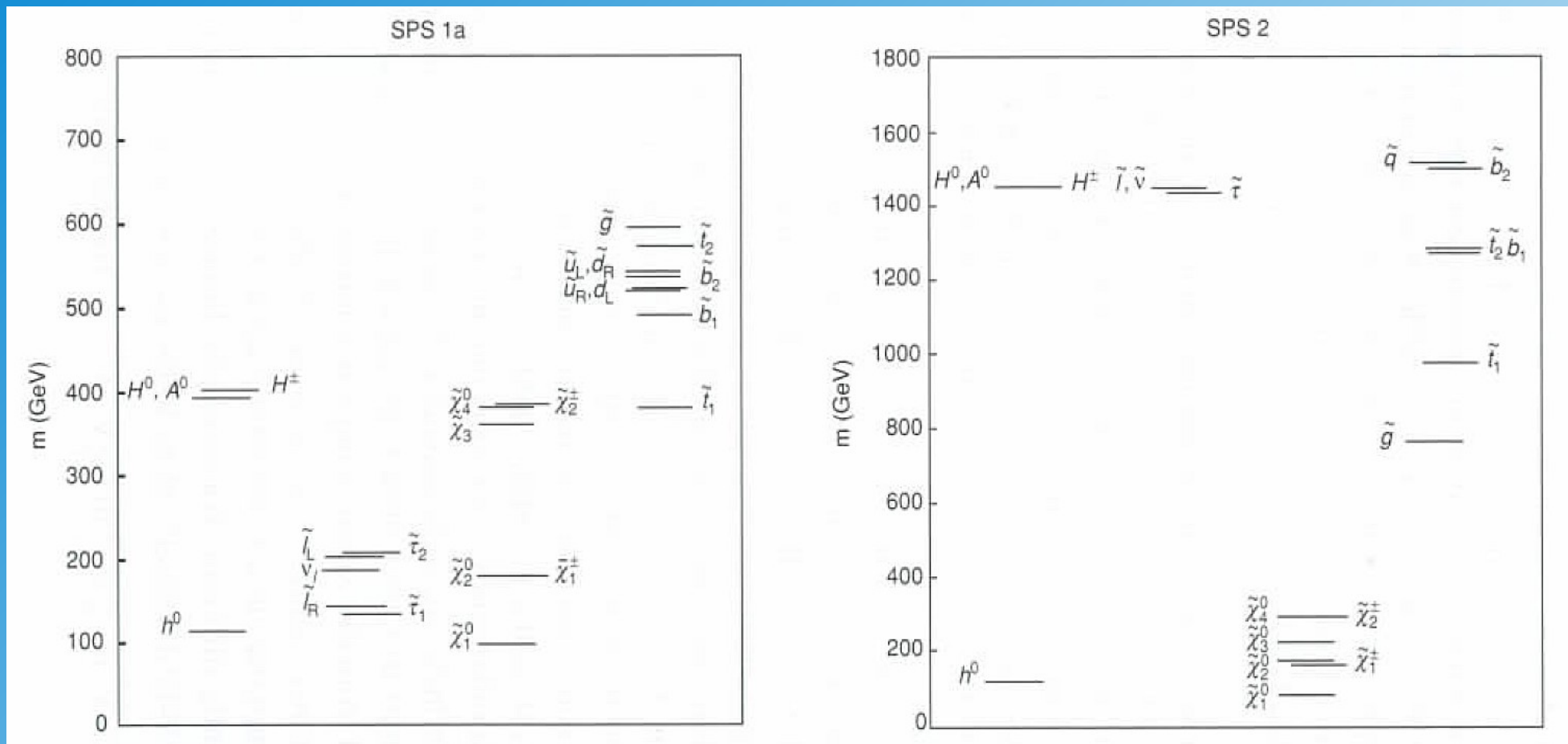


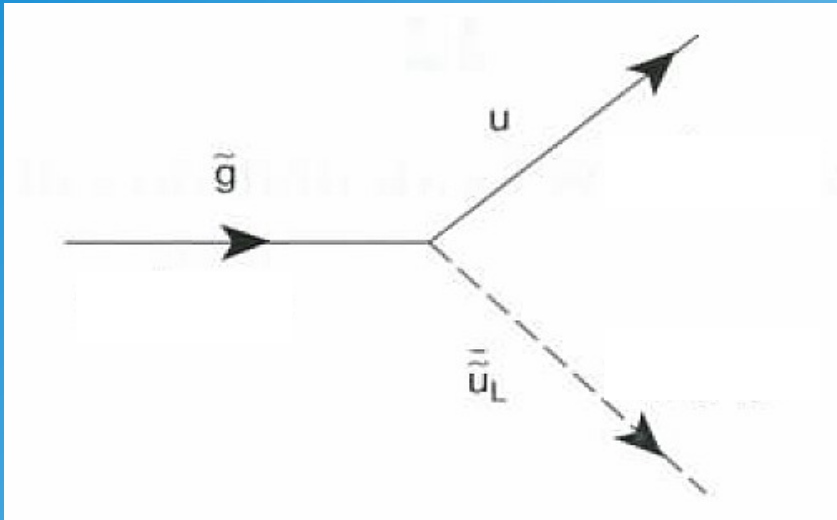
Figure 12.10 The SUSY particle spectra for the benchmark points corresponding to the parameter values SPS 1a (equation (12.155)) and SPS 2 (equation (12.156)). [From B. C. Allanach, *et al.*, *Eur. Phys. J. C* **25** Figure 1, p. 118 (2002), reprinted with the permission of Springer Science and Business Media.]

comparison of two different parameters sets (“Snowmass Points”)

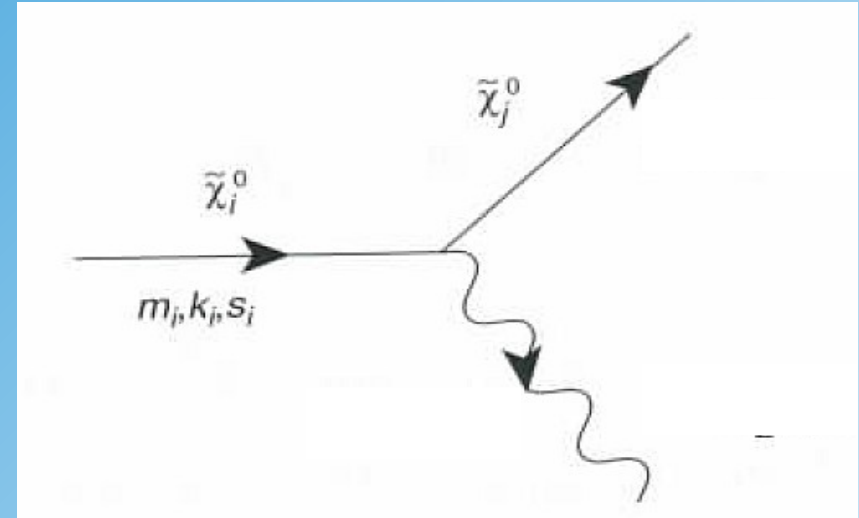
both are excluded in the meantime...

# SUSY $R_P$ -Conserving Couplings

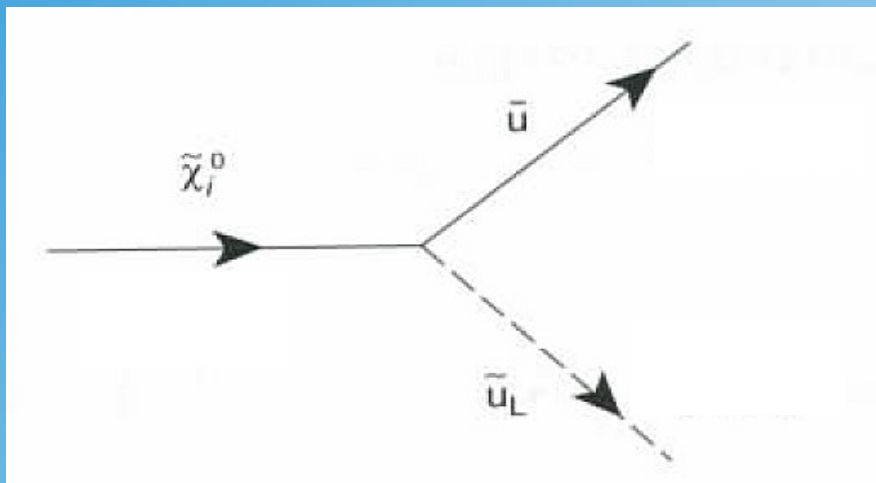
Glino-squark-quark:



Neutralino-Neutralino-Z-boson:



Neutralino-squark-quark:



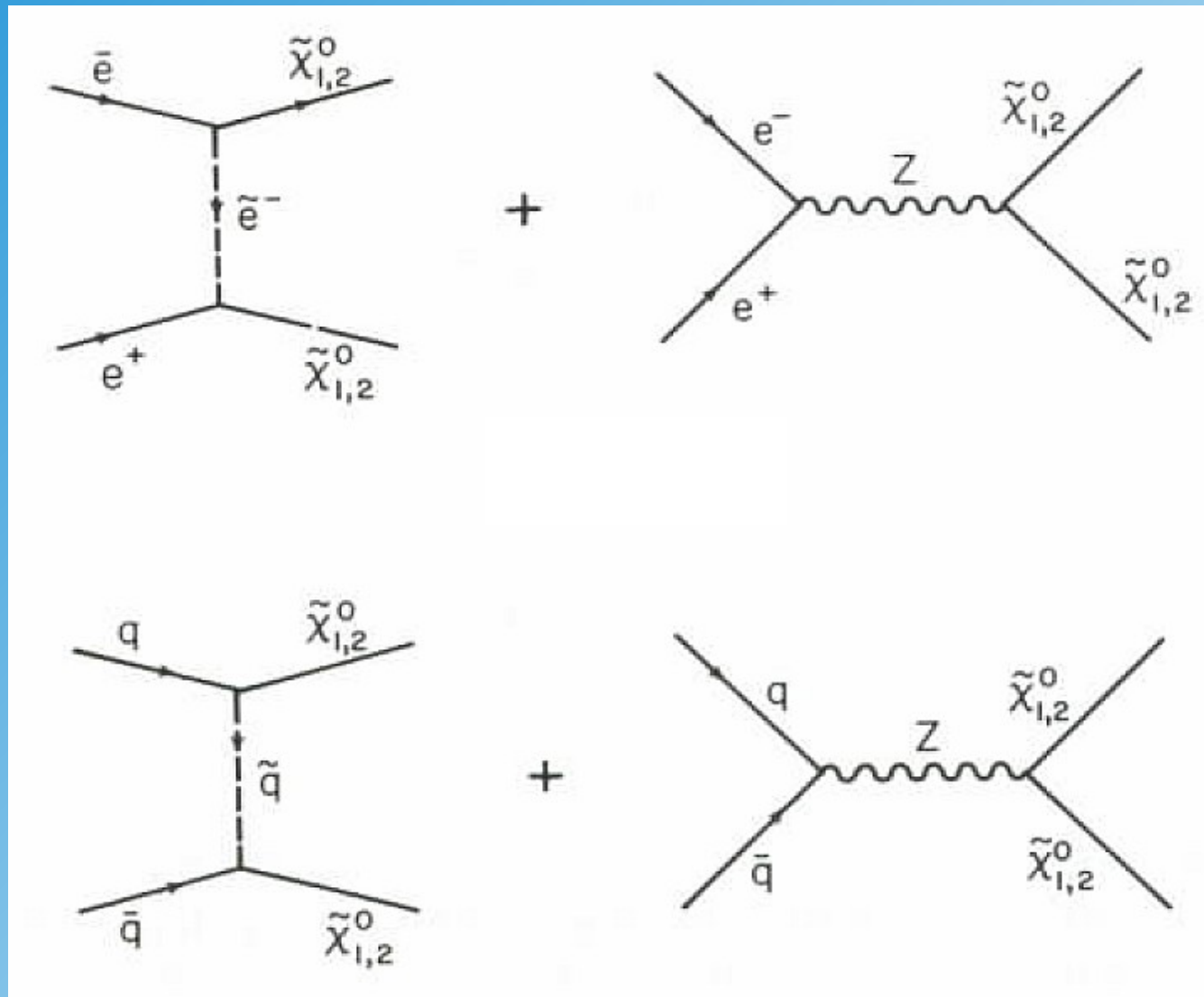
$$R|SM\rangle = 1 \quad R|SUSY\rangle = -1$$

- $R_P$  is a multiplicative quantum number
- if conserved SUSY particles can only be produced in pairs and “SUSYness” is conserved in decays

$$\text{relation: } R = (-1)^{3B+L+2S}$$

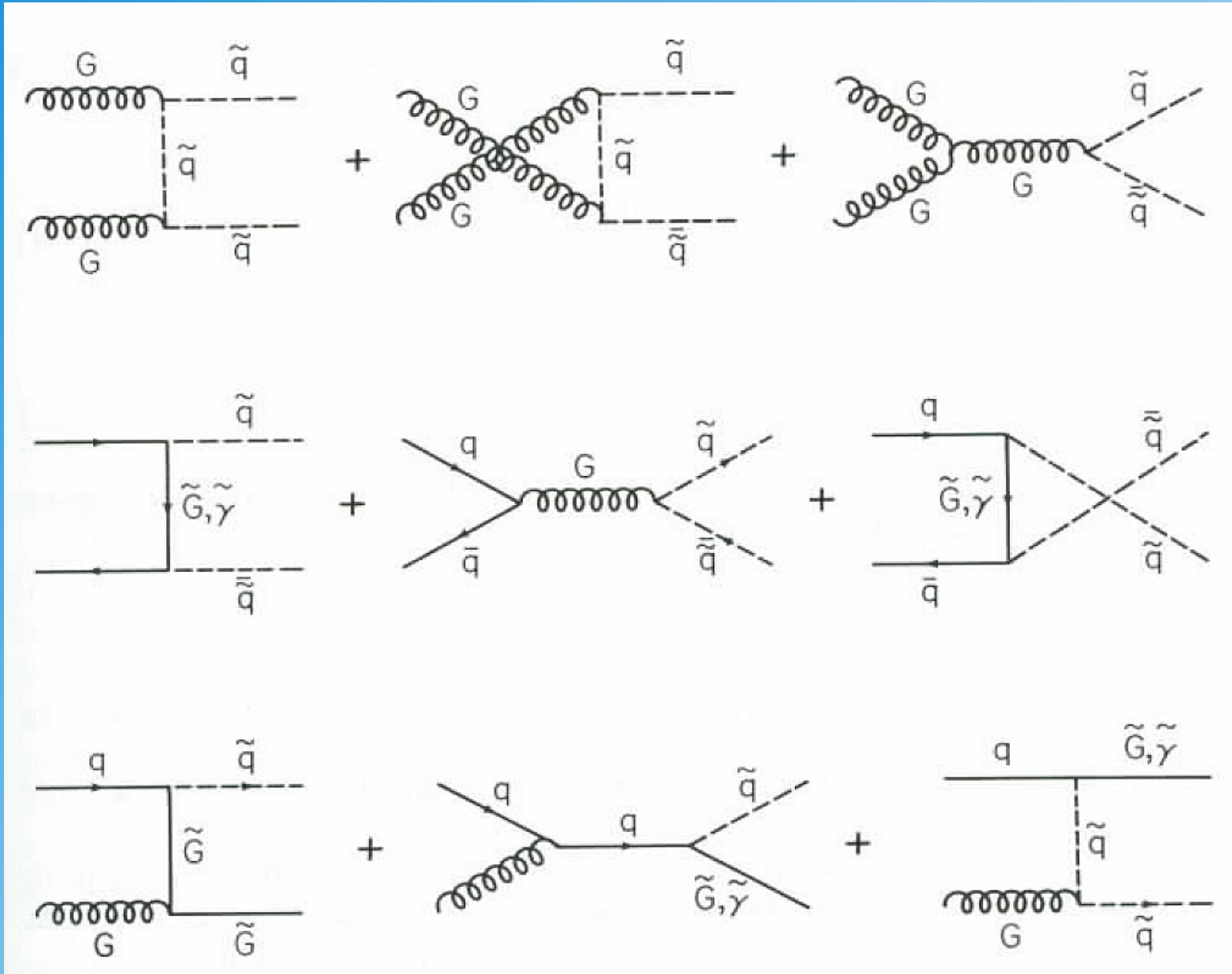
# SUSY Feynman Graphs

Neutralino Pair-Production:



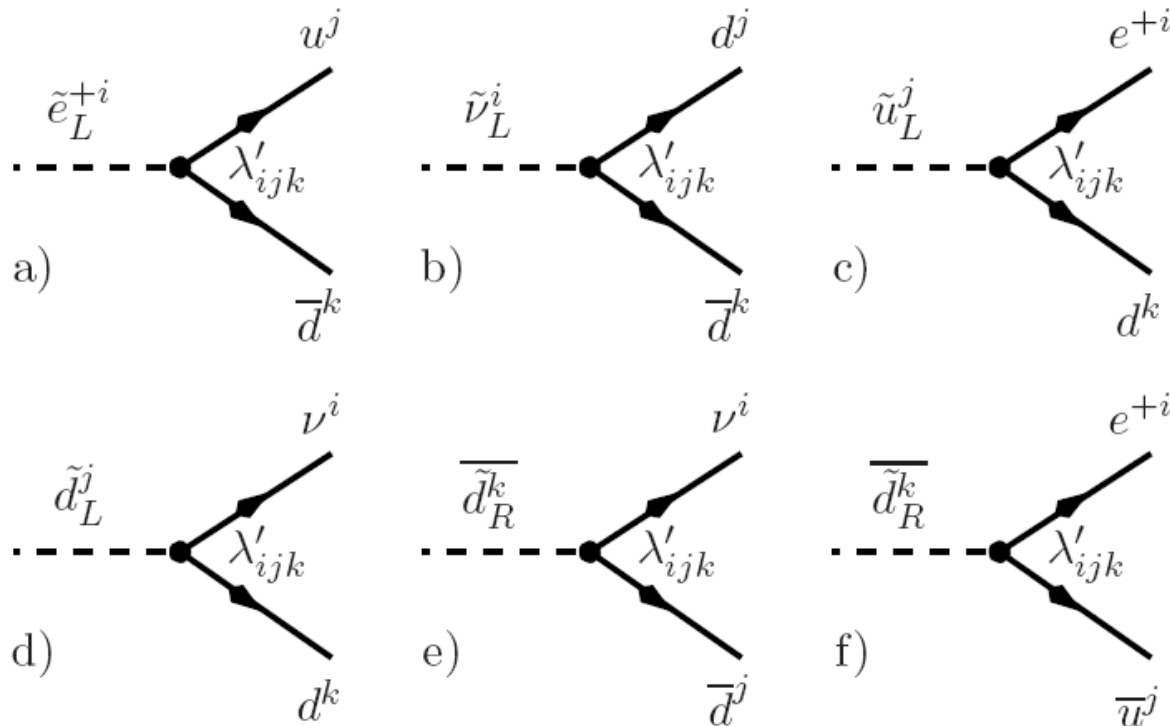
# SUSY Feynman Graphs

SUSY production in hadron interactions (e.g. LHC)



# R-Parity Violating Couplings

Trilinear RPV-Yukawa Couplings:



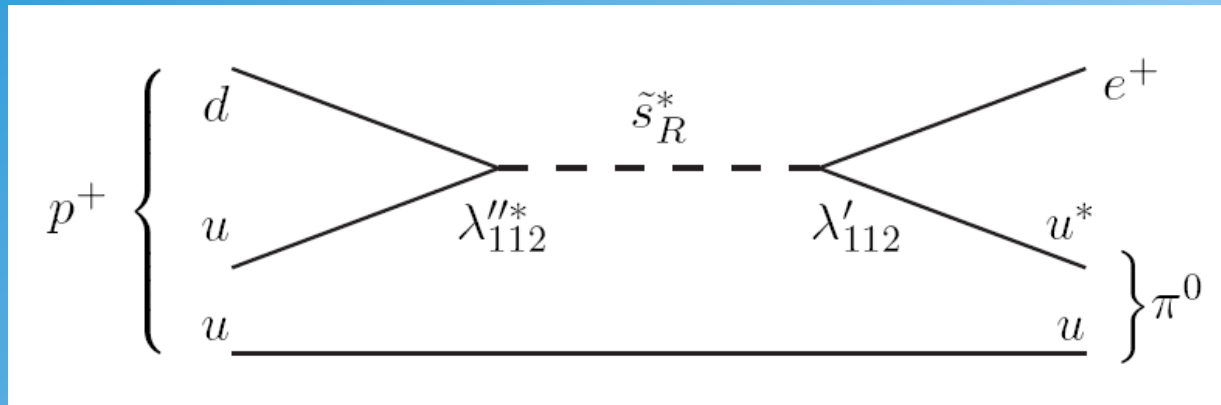
lightest  
SUSY particle  
(dark matter  
candidate!)  
not stable

$$\mathcal{L}_{L_i Q_j \bar{D}_k} = \lambda'_{ijk} \left[ -\tilde{e}_L^i u_L^j \bar{d}_R^k - e_L^i \tilde{u}_L^j \bar{d}_R^k - (\tilde{e}_L^i)^c u_L^j \bar{d}_R^{k*} \right. \\ \left. + \tilde{\nu}_L^i d_L^j \bar{d}_R^k + \nu_L^i \tilde{d}_L^j \bar{d}_R^k + (\tilde{\nu}_L^i)^c d_L^j \bar{d}_R^{k*} \right] + \text{c.c.}$$

RPV sparticles decay:  $\Gamma_{RPV} = \frac{1}{16\pi} \lambda_{ijk}^2 M_{\tilde{q}}$  (but could be long-lived)

# L,B Number Violation and R-Parity

if R-parity is violated with first generation couplings  $\Delta L=1$  and  $\Delta B=1$ , the proton would undergo a catastrophic decay:



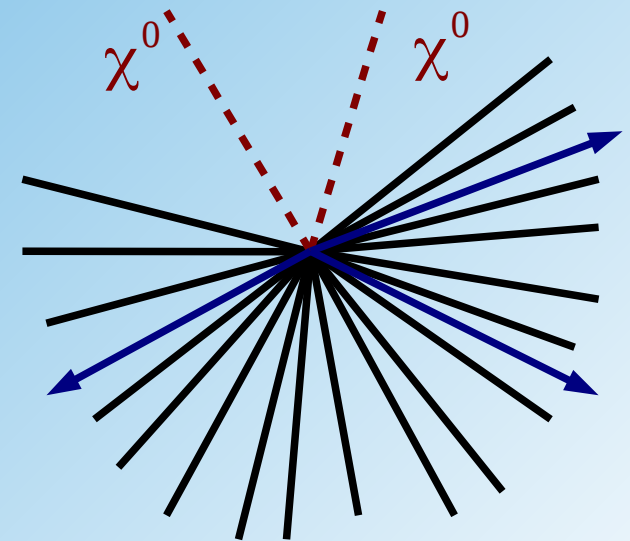
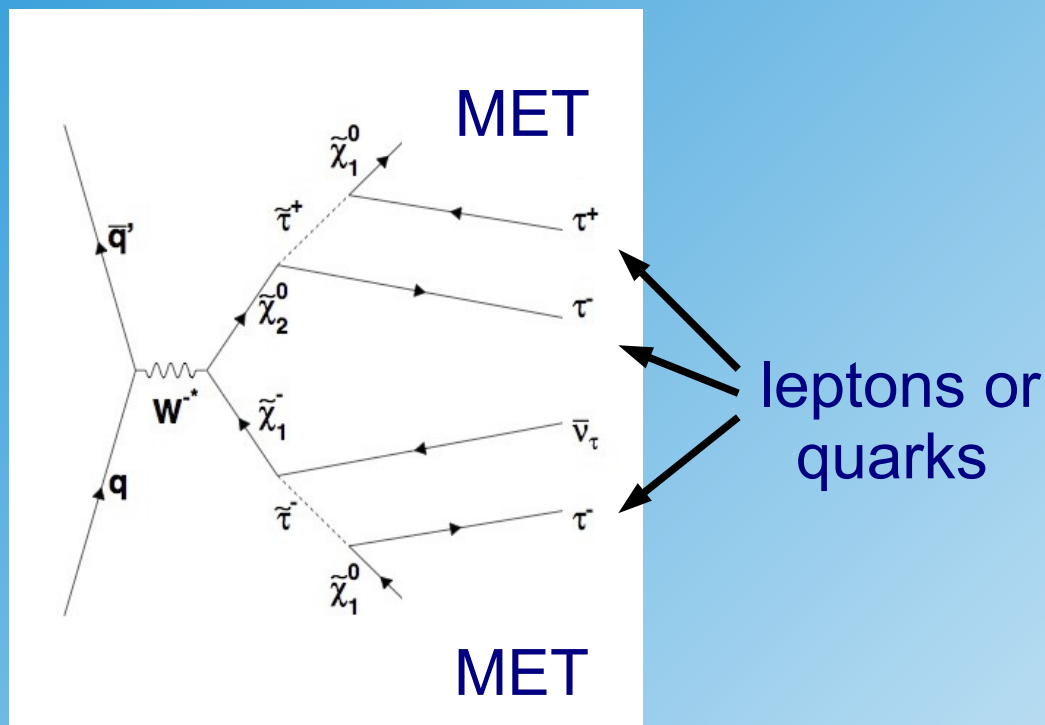
$$L_{\Delta L=1} = \frac{1}{2} \lambda^{ijk} L_i L_j \bar{e}_k + \lambda'^{ijk} L_i Q_j \bar{d}_k + \mu^i L_i H_u$$

$$L_{\Delta B=1} = \frac{1}{2} \lambda''^{ijk} \bar{u}_i \bar{d}_j \bar{d}_k$$

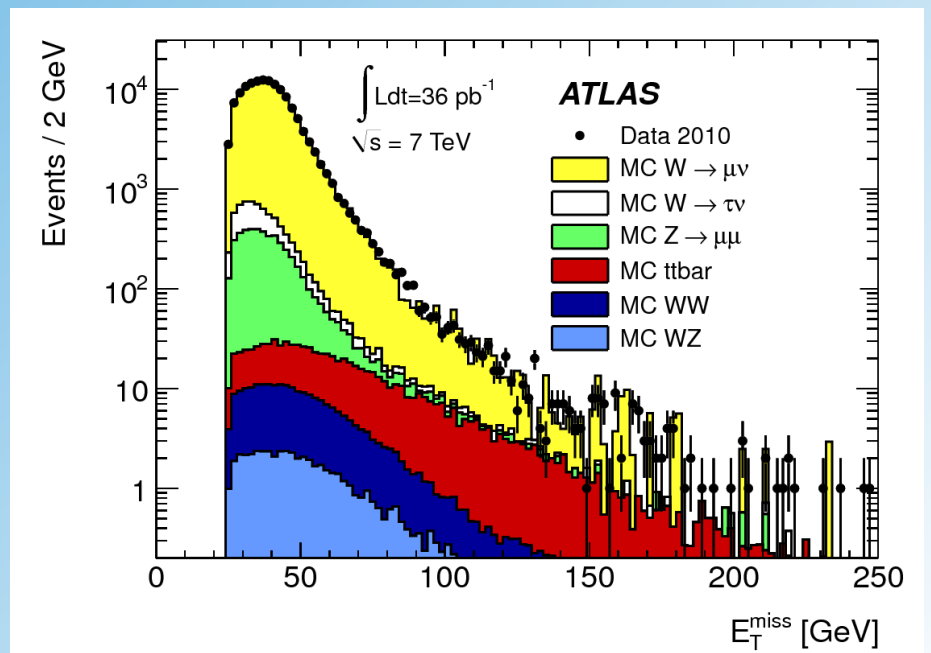
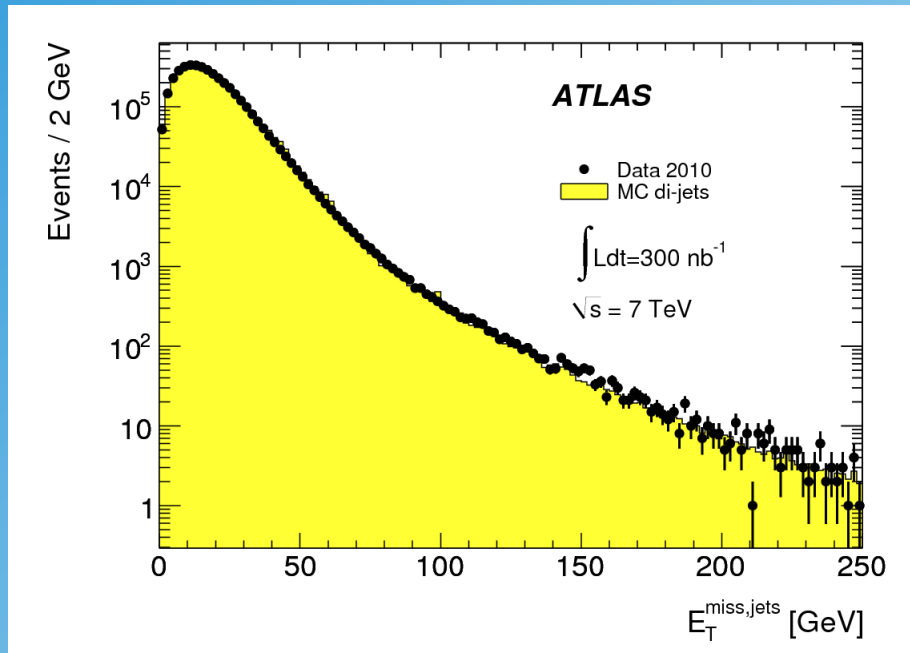
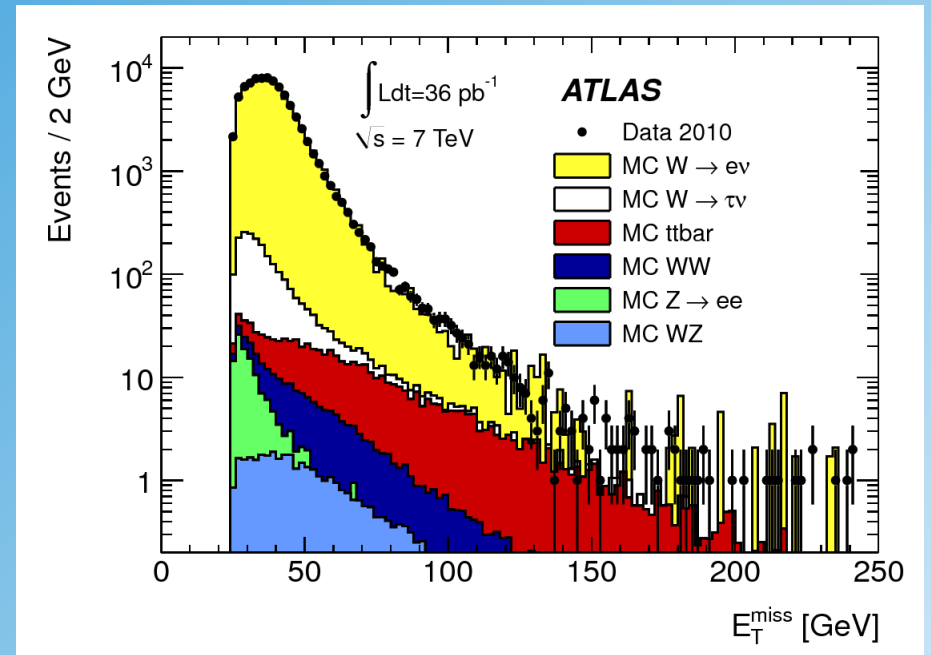
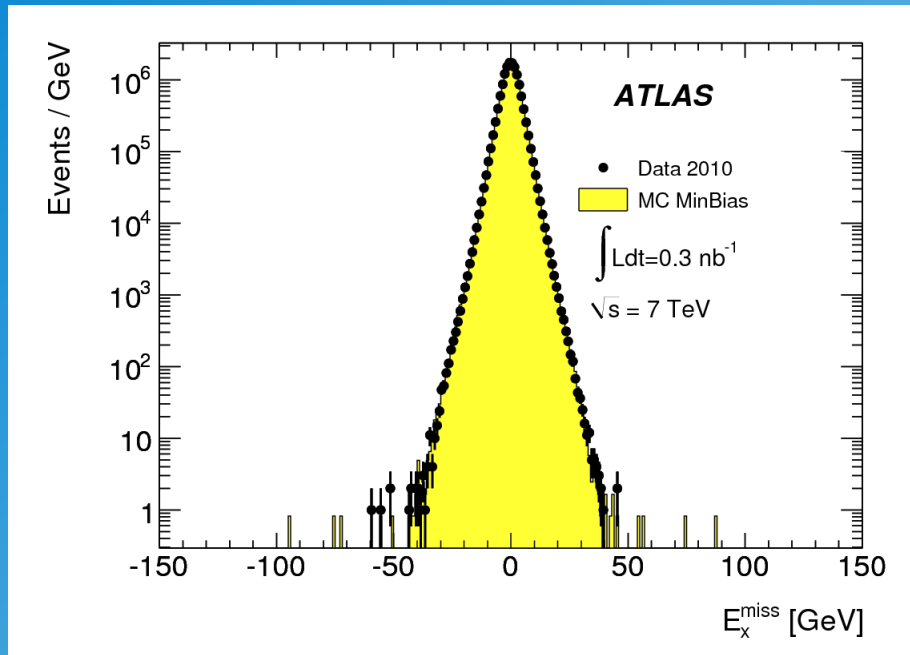
RP-Violating couplings are not excluded in general  
but many combinations of non-zero terms are constrained!

# Experimental Search Strategy at LHC

- Assumption:  $R_p$  is conserved
- SUSY particles produced in pairs will decay in cascades
- In many models the neutralino is the lightest SUSY particle and stable
- The neutralino escapes detection and leads to missing energy in the detector

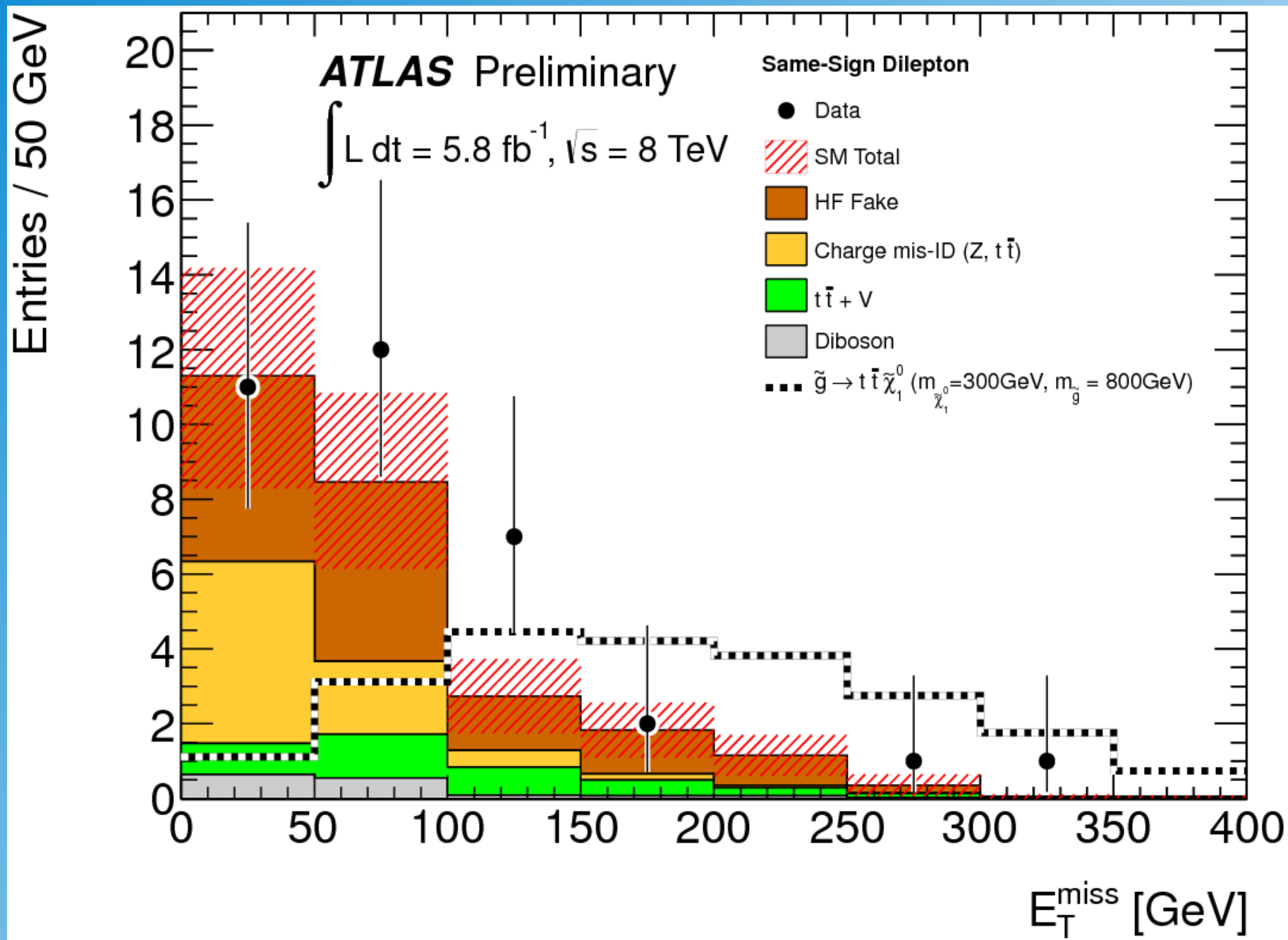


# $E_T^{\text{miss}}$ Performance



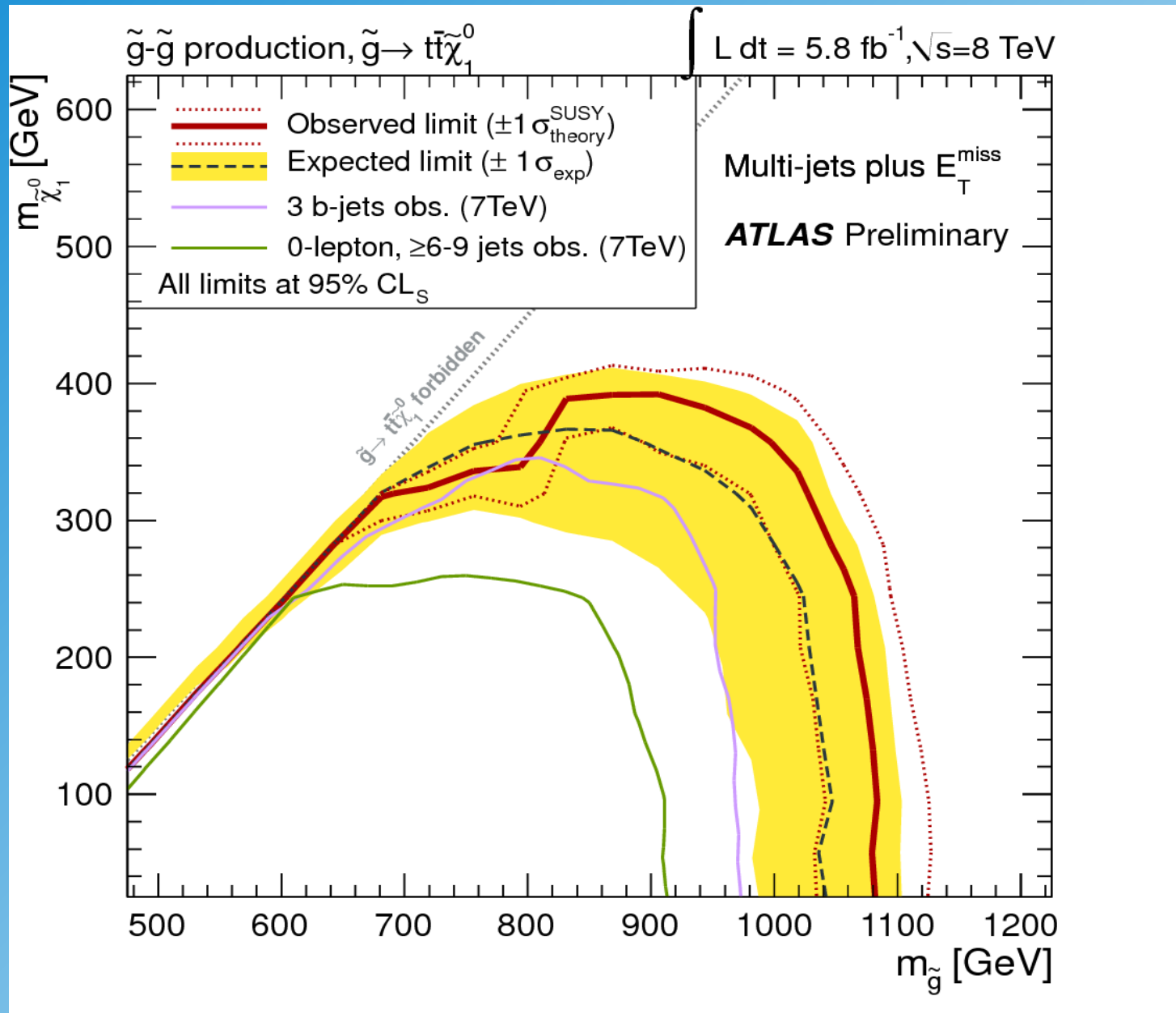


# Same Charge Dilepton Sample

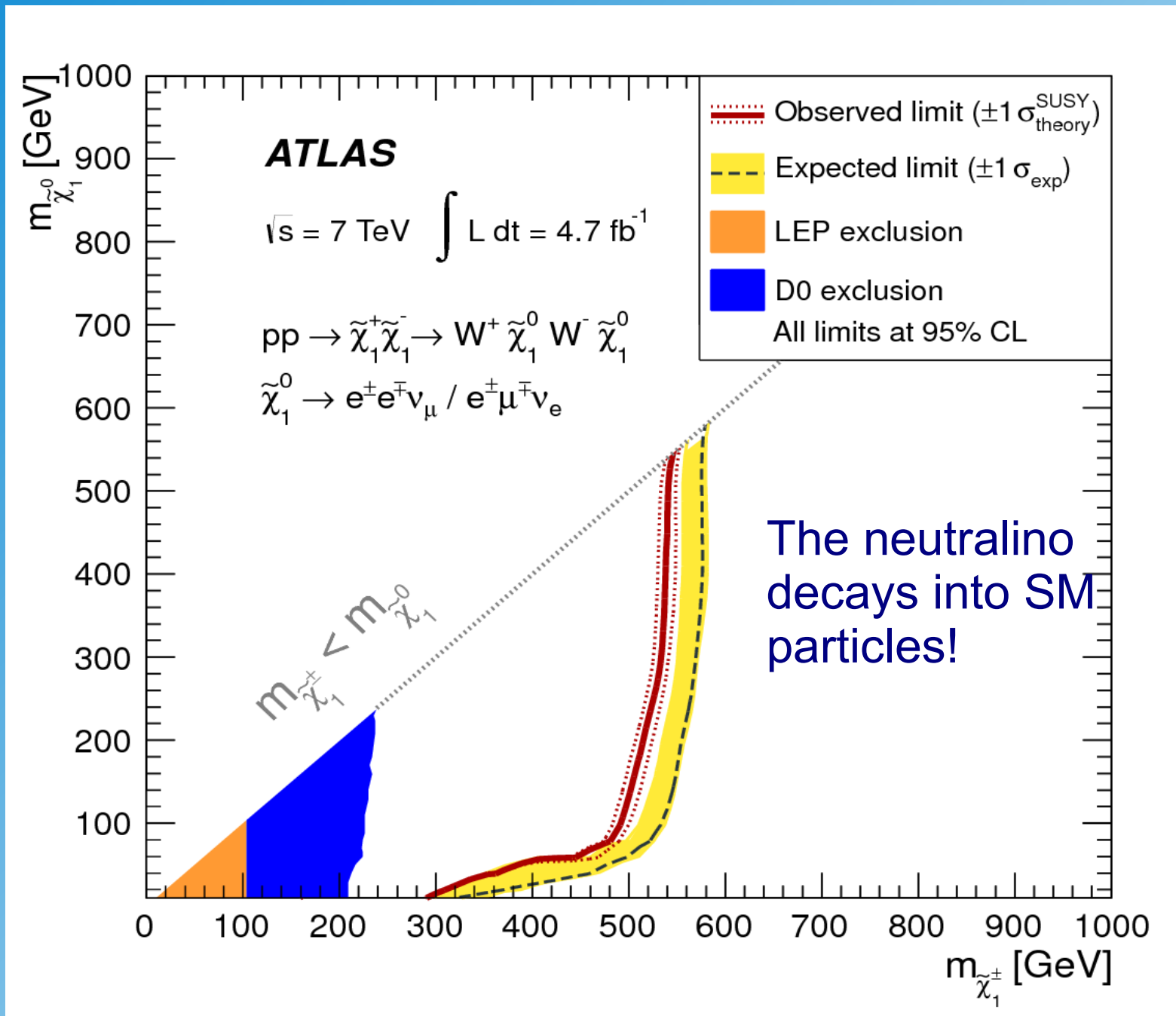




# Search for SUSY in Top-Quark Final States without Leptons

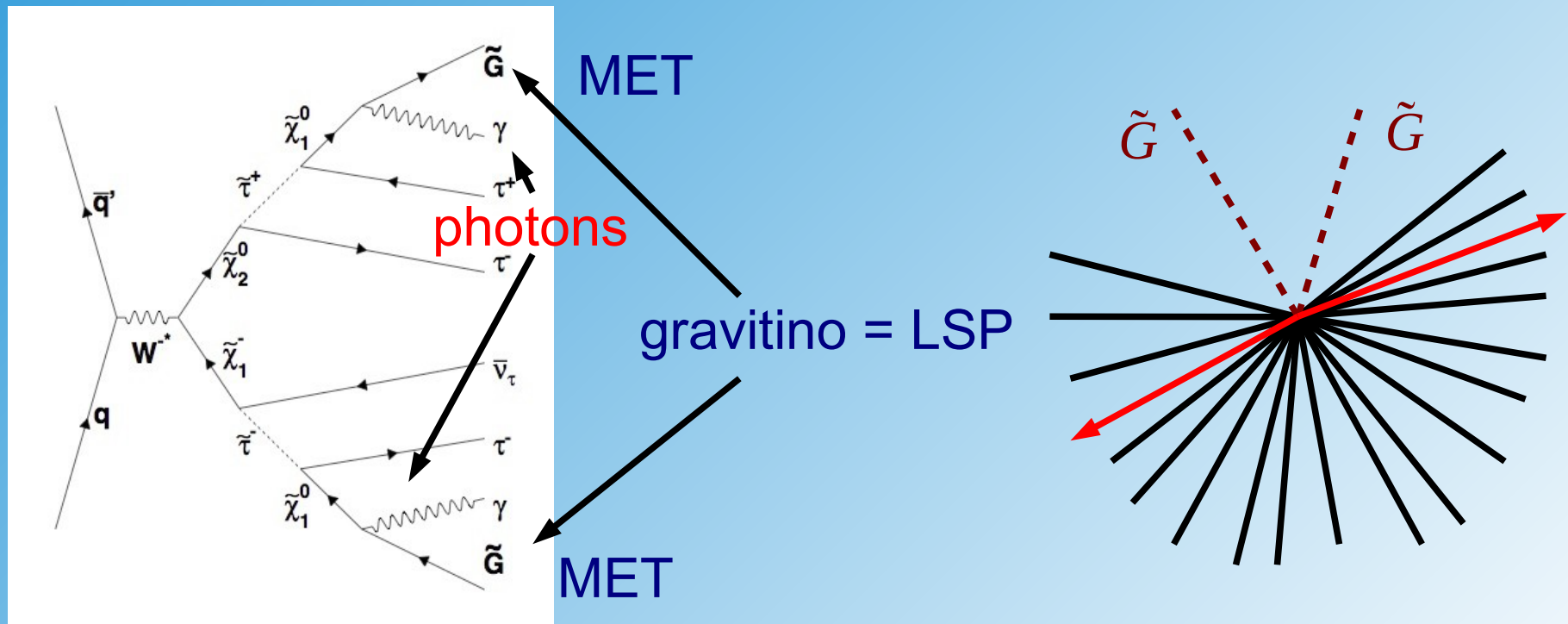


# R<sub>P</sub> Violation (RPV) Searches

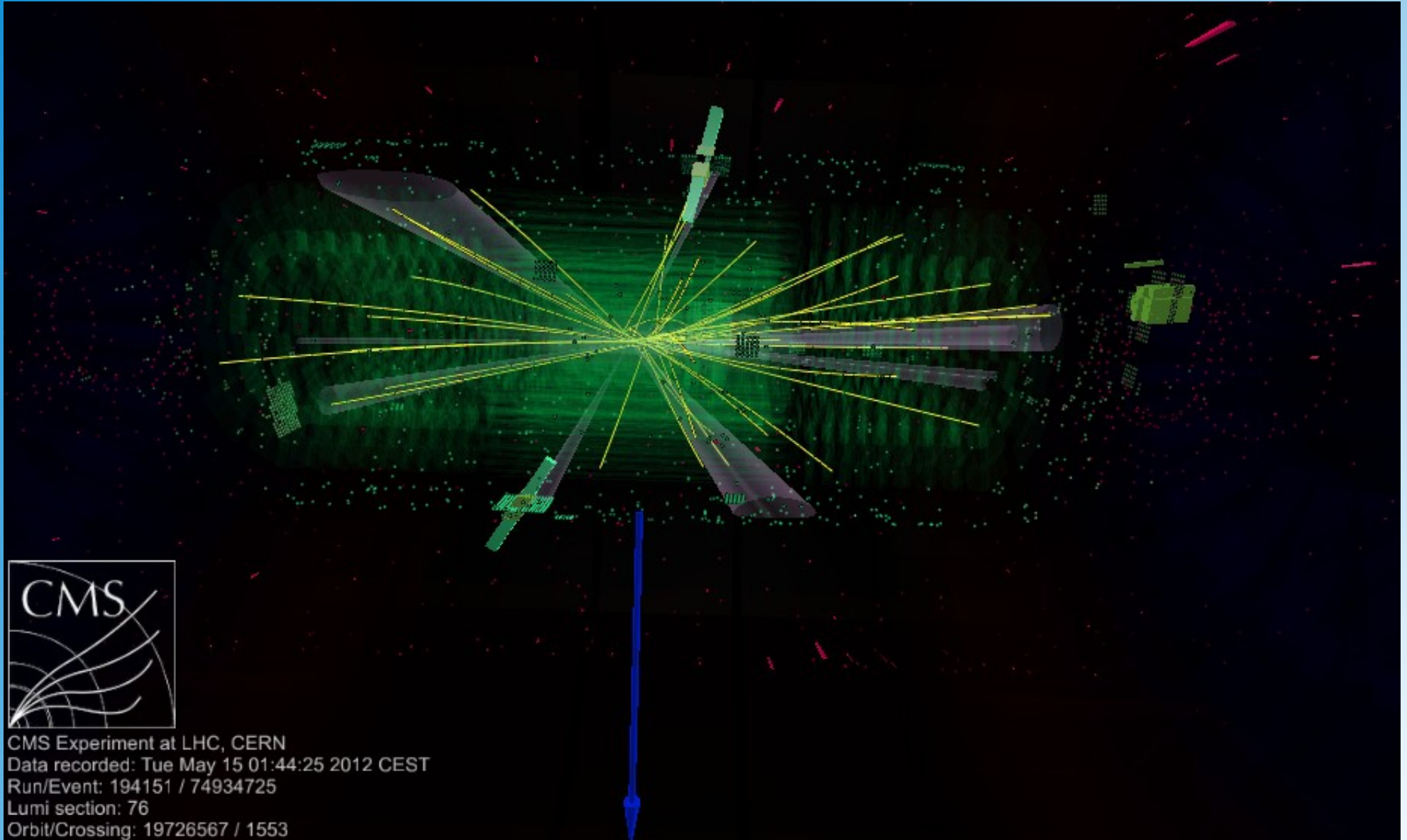


# Search for GMSB-SUSY at LHC

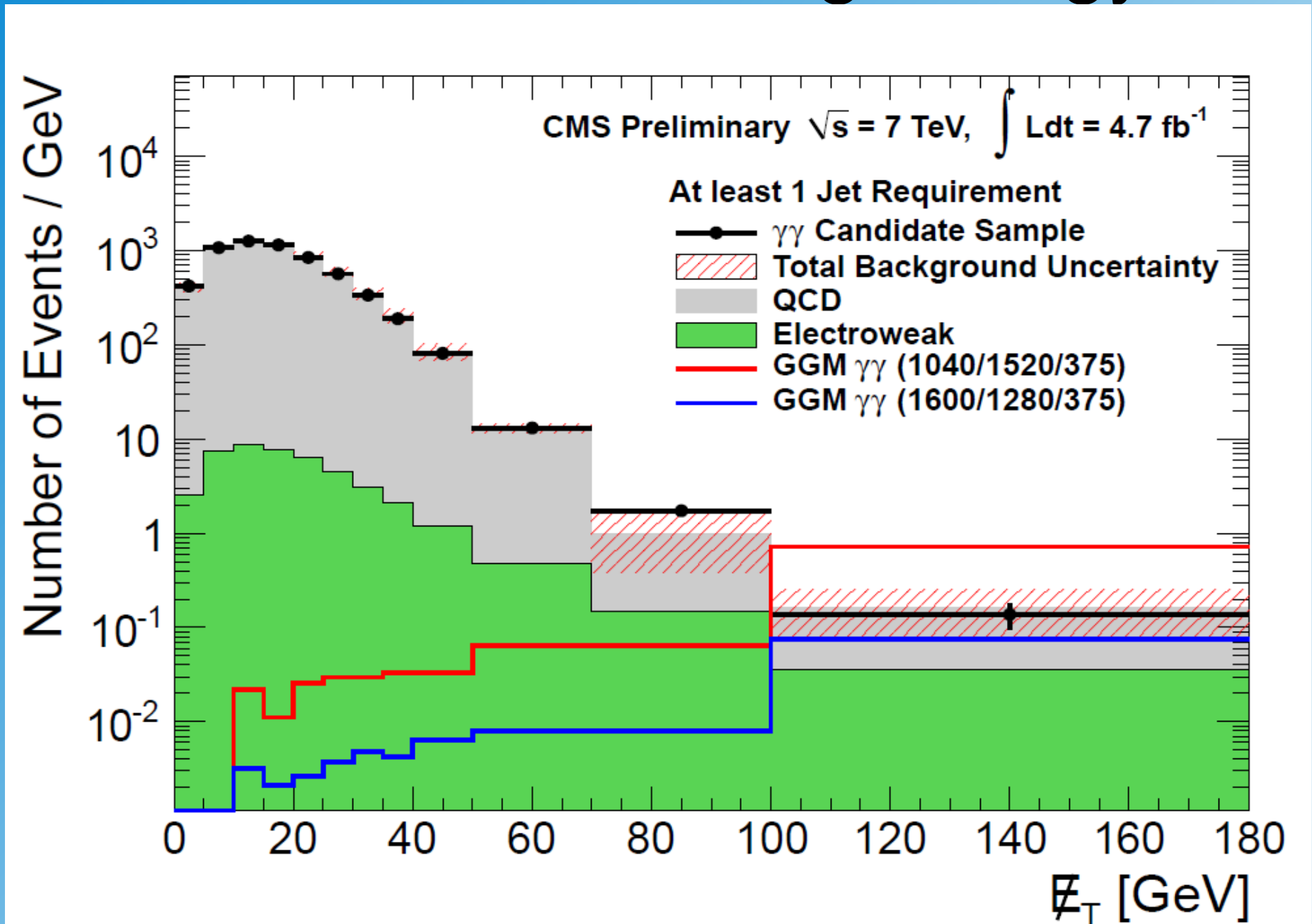
- Assumption:  $R_p$  is conserved
- In GMSB models the gravitino is the LSP (can be very light!)
- The neutralino is the NLSP and decays to photon and gravitino
- Search Topology: MET + photons



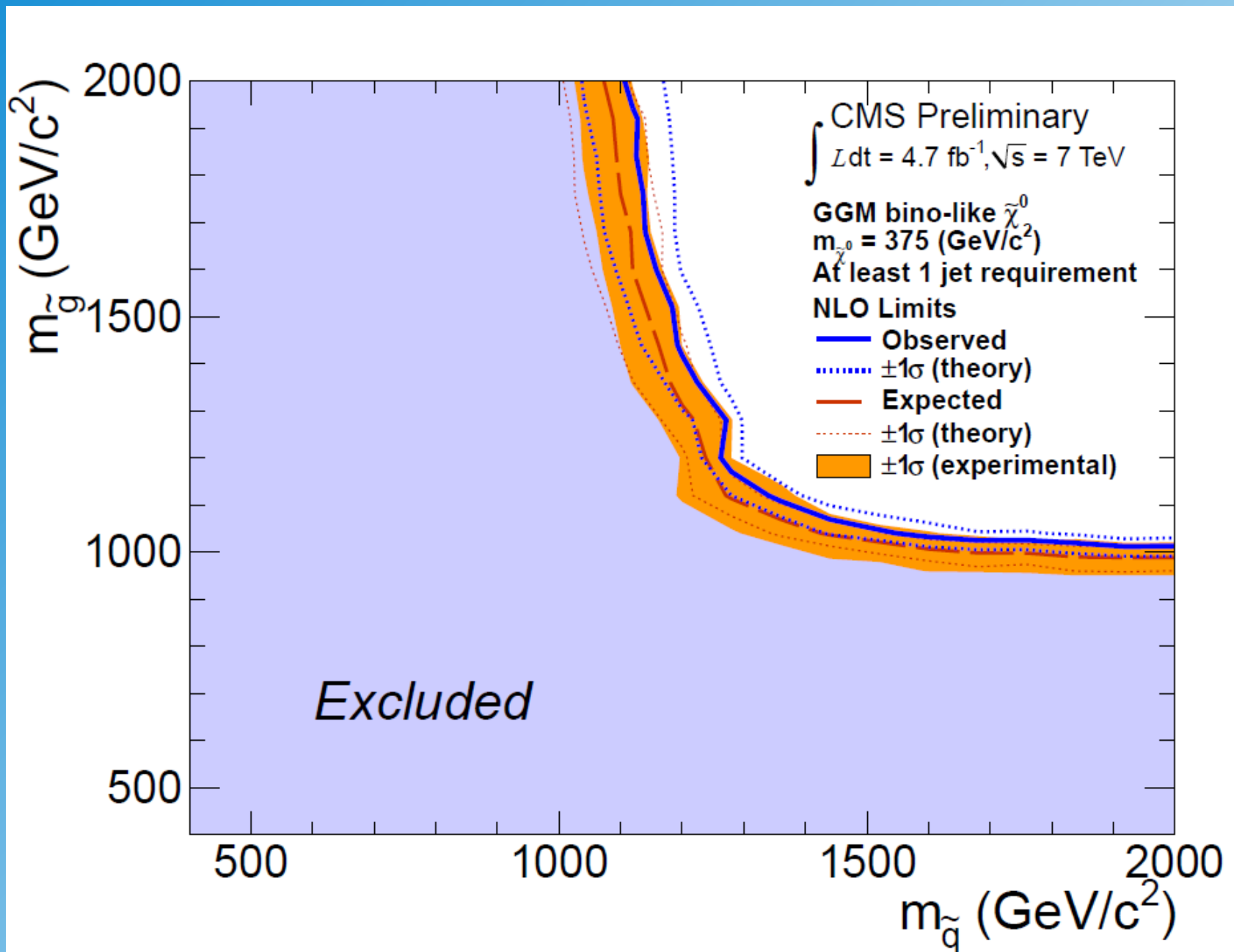
# CMS Two Photon Event



# Di-Photon Missing Energy

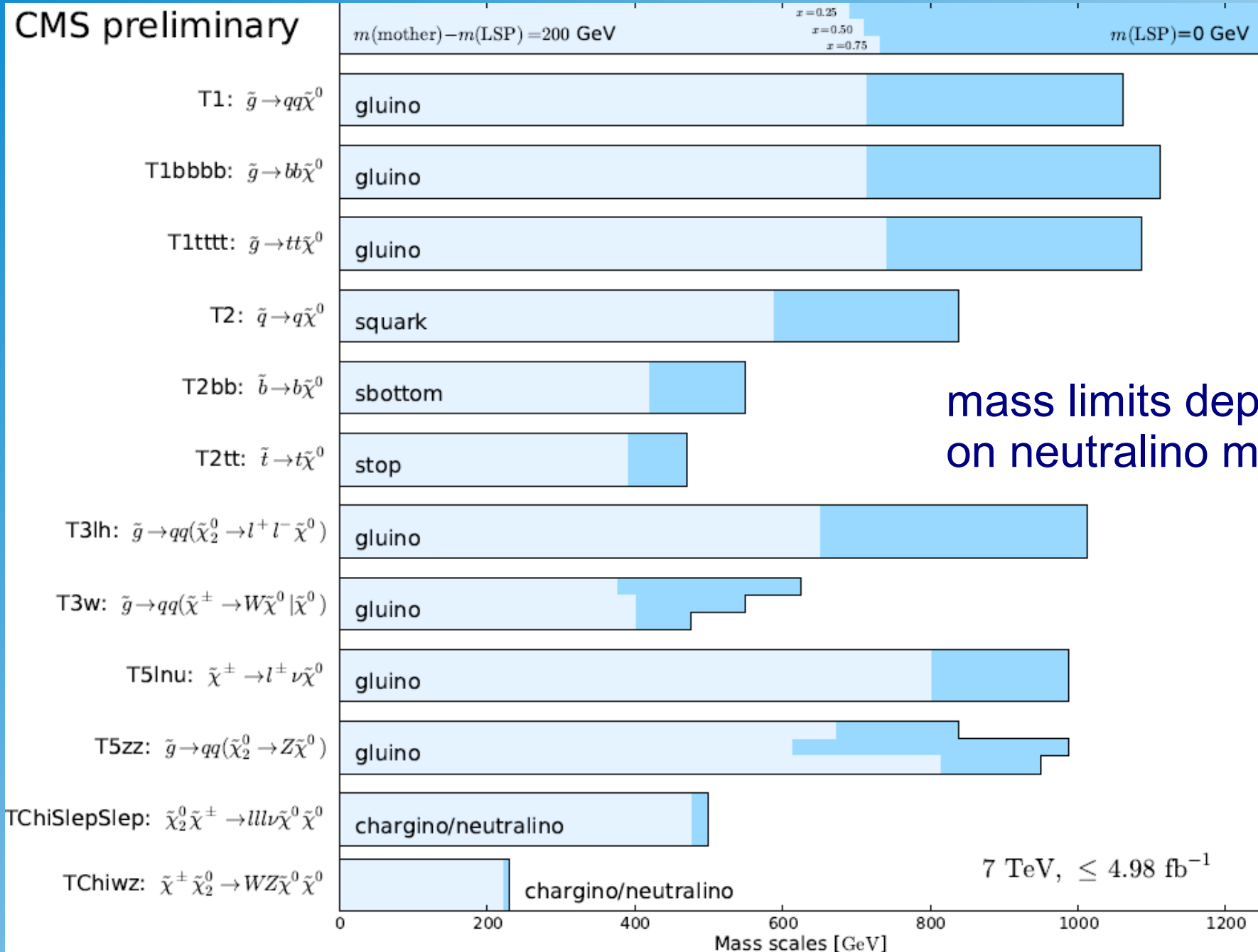


# CMS Results (GMSB)





# Overview CMS Results (MSSM)



# Other SUSY Searches

## Discussed:

- MSSM SUSY searches with neutralino in final state (missing  $E_T$ )
- Searches with photons and gravitinos in final state (missing  $E_T$ )
- Searches with same-charge leptons and missing  $E_T$
- Searches with R-parity violation

## Not Discussed:

- Many more (complex) topologies exist and studied
- SUSY particles could be long-lived and massive (highly ionizing)
- SUSY particles could decay half way in the detector (kinks)
- SUSY particles could form R-hadrons (SUSY-hadrons) which interact in the detector
- and, and, and ....

# Summary

- **Despite the fact that the cross section for the production of light SUSY particles is large at LHC, no sign of SUSY seen yet (in most simple models and analysis)**
- **Searches will continue with larger datasets and at higher beam energies ( $\sqrt{s}=14$  TeV). More complex models will be studied. Main problem is that the mechanism of SUSY breaking is unknown.**
- **SUSY cannot experimentally ruled at at LHC if the SUSY mass scale is large. However, than it would not solve the fine tuning problem.**

